

Sensorless Control with Kalman Filter on TMS320 Fixed-Point DSP

Literature Number: BPRA057
Texas Instruments Europe
July 1997

IMPORTANT NOTICE

Texas Instruments (TI) reserves the right to make changes to its products or to discontinue any semiconductor product or service without notice, and advises its customers to obtain the latest version of relevant information to verify, before placing orders, that the information being relied on is current.

TI warrants performance of its semiconductor products and related software to the specifications applicable at the time of sale in accordance with TI's standard warranty. Testing and other quality control techniques are utilized to the extent TI deems necessary to support this warranty. Specific testing of all parameters of each device is not necessarily performed, except those mandated by government requirements.

Certain applications using semiconductor products may involve potential risks of death, personal injury, or severe property or environmental damage ("Critical Applications").

TI SEMICONDUCTOR PRODUCTS ARE NOT DESIGNED, INTENDED, AUTHORIZED, OR WARRANTED TO BE SUITABLE FOR USE IN LIFE-SUPPORT APPLICATIONS, DEVICES OR SYSTEMS OR OTHER CRITICAL APPLICATIONS.

Inclusion of TI products in such applications is understood to be fully at the risk of the customer. Use of TI products in such applications requires the written approval of an appropriate TI officer. Questions concerning potential risk applications should be directed to TI through a local SC sales office.

In order to minimize risks associated with the customer's applications, adequate design and operating safeguards should be provided by the customer to minimize inherent or procedural hazards.

TI assumes no liability for applications assistance, customer product design, software performance, or infringement of patents or services described herein. Nor does TI warrant or represent that any license, either express or implied, is granted under any patent right, copyright, mask work right, or other intellectual property right of TI covering or relating to any combination, machine, or process in which such semiconductor products or services might be or are used.

Contents

1. Notation and Symbols	1
2. The Hardware	2
3. The Field Oriented Control Method	3
4. Motor Model Used in the Field Oriented Control	4
5. Implementation of the Field Oriented Control Method.....	6
6. Kalman Filter	9
7. Basics of Observers	10
8. Basics of Kalman Filters.....	12
9. Motor Model for the Kalman Filter	14
10. Simulation of the Kalman Filter.....	17
11. Simulation Results	18
12. Real-Time Implementation of the Kalman Filter.....	21
13. Real Time Results	27
14. Conclusions and Possible Development.....	29
References.....	30
Appendix Source Code of Programs	32

List of Figures

Figure 1: New Control Hardware System	3
Figure 2: Model 1 - Field Oriented Controller for the ASM.....	8
Figure 3: Reconstruction of the State Vector.....	10
Figure 4: Structure of the Luenberger Observer	11
Figure 5: Model 2 - Controller with Kalman Filter.....	18
Figure 6: Speed Reversal with FOC.....	19
Figure 7: Speed Reversal with EKF	19
Figure 8: Applying Load at 0 RPM with FOC.....	20
Figure 9: Applying Load at 0 RPM with EKF	20
Figure 10: Speed Reversal with Kalman Filter	27
Figure 11: Speed Reversal with Speed Measurement.....	28

List of Tables

Table 1: Summary of Notational Conventions.....	2
Table 2: Some Types of Matrix Multiplication Needed For Kalman Filter	23
Table 3: Scaling Factors of Variables	25
Table 4: Constant Values	25
Table 5: Memory Requirements of Kalman Filter.....	28

Sensorless Control with Kalman Filter on Fixed-Point DSP

ABSTRACT

The importance of Digital Motor Control (DMC) has grown gradually. As Digital Signal Processors have become cheaper, and their performance greater, it has become possible to use them for controlling electrical drives as a *cost effective* solution. Some relatively new methods such as speed sensorless field oriented control utilize this enhanced processing capacity. This document discusses the implementation of a *sensorless* field oriented control for induction motors using the Kalman Filter. First the theory of field oriented methodology, with and without speed sensor, is described. Then a simulation approach is given for both cases. Finally the real-time implementation issues of a sensorless control are discussed. The paper presents an evaluation of the results. The processing capability of the processor is used to 50% at the current cycle times, the memory requirement is approximately 6823 Word program, and 2564 Word data space, of which 1024 Words are C-stack. The appendix contains full source code of the sensorless control for the TMS320C50¹ DSP, which is source compatible to the other members of the Fixed-Point DSP family like 'C1x, 'C2xx.

1. Notation and Symbols

In this chapter the notational conventions will be summarized, as used in this document. Throughout this work notations used by [6] (University Paderborn), [7] (dSPACE) and [4] (Beierke) will be followed. The internal variable notations of the programs will not be discussed here. The meanings of the variables are documented in the corresponding programs.

¹ In this document we will use the following abbreviations: C14 for TMS320C14, C50 for the TMS320C50 etc.

Table 1: Summary of Notational Conventions

Meaning	Notation
Electrical and Mechanical Torque	m_e, m_L
Fluxes ²	Ψ
Flux Angle	ρ or ε_{FS}
Flux Speed	ω_{mR} or ω_{FS}
Inertia	J
Leakage Factor	$\sigma = \frac{K_L}{L_S}$
Stator and Rotor Leakage Factor	σ_R, σ_S
Magnetic Pole Count	z_p or p
Magnetizing current	i_{mR}
Phase Currents	i_a, i_b, i_c
Rotor, Stator and Main Inductances	L_R, L_S, L_H
Rotor and Stator Resistances	R_R, R_S
Rotor and Stator Time Constants	T_R, T_S
Rotor Angle	ε or ε_{RS}
Rotor Currents Scalar Components	$i_{R\alpha}, i_{R\beta}$
Rotor Speed	ω or ω_{RS}
Stator and Rotor Currents	$\underline{i}_R, \underline{i}_S$
Stator Currents in Field Coordinates	i_{sd}, i_{sq}
Stator Currents Scalar Components	$i_{S\alpha}, i_{S\beta}$
Voltages ³	u

Note, that in most of the articles about field oriented control rotor flux is regarded simply as “flux” and this document will follow this convention as well.

2. The Hardware

This chapter will give a very short overview of the hardware used in this project. This motor controller card (see Figure 1 on page 3) is based on a TMS320C50 DSP (Digital Signal Processor) manufactured by Texas Instruments. Other main elements of the system are a UART for serial communication with a PC or VT-100 terminal, an A/D converter with an analog multiplexer, which can be used to input up to 8 channels of analog signals in the range of 0-5V, a PWM generator, which is implemented inside an FPGA of Texas Instruments, a GPIO unit, with an integrated incremental encoder interface. All this features are now integrated in a new device called DSP-Controller TMS320C240.

²Indices are just the same as for currents

³Indices are just the same as for currents

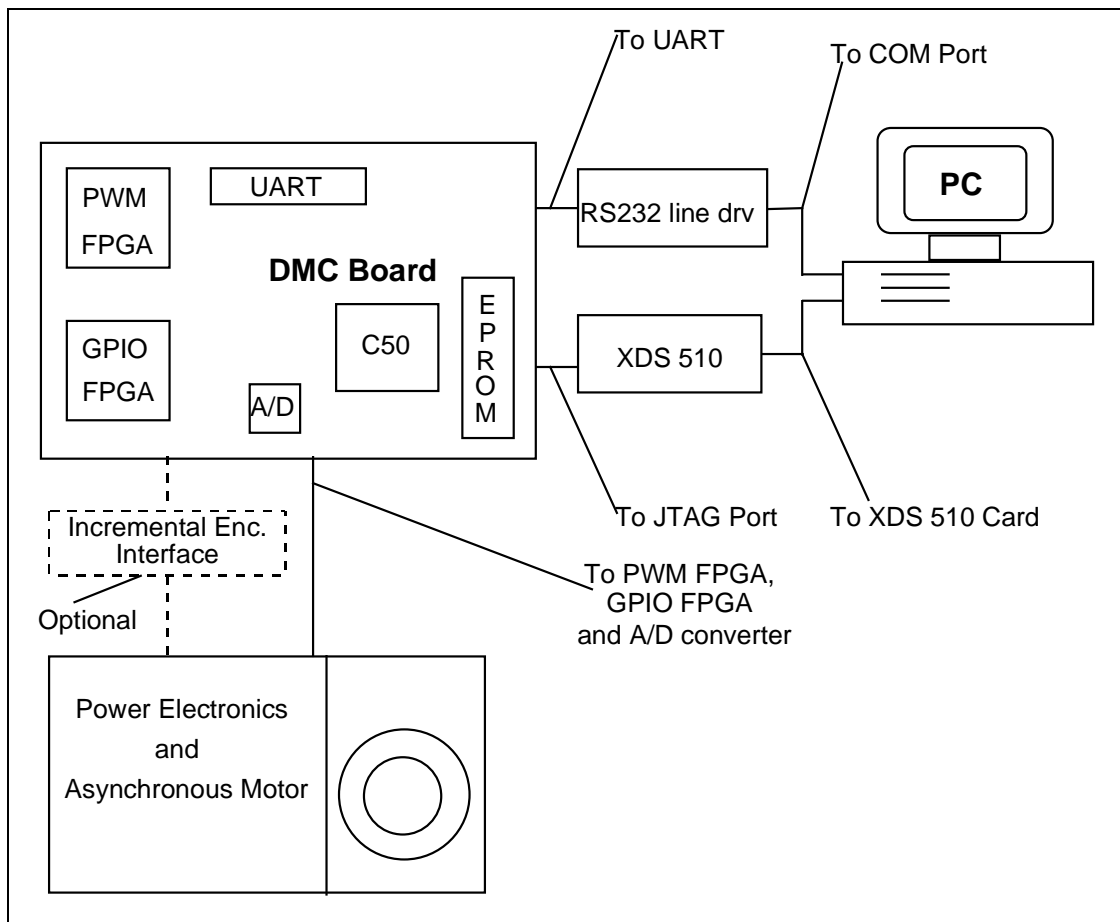


Figure 1: New Control Hardware System

3. The Field Oriented Control Method

In the case of an asynchronous 3 phase motor, sometimes regarded as an induction cage motor, a very elegant control method, the field oriented control is available. The main feature of this method is that all variables are converted to the coordinate system of the magnetic field of the rotor, called the rotor flux. The flux is held constant using the current component parallel to the rotor flux (i_{sd}), the torque is controlled by the other current component (i_{sq}). This method is basically the same as controlling separately excited DC motors. The control method is not very complicated, however the calculation of the rotor flux and a conversion of the variables from the stator system to the flux system requires high processor capacity, since a conversion between field coordinates and stator coordinates is needed in both directions in each controlling cycle. The C14 DSP was completely capable of doing this job in real time. The motor and the controlling hardware is relatively cheap, on the other hand the software is quite complicated. But this complicated software can be used in a quite flexible way, once it is developed.

The main reason for using this method is its dynamic performance. Specifically, it offers good lead performance, and resistance against disturbances such as changes of the load torque. These properties can be achieved by a decoupling of the flux and the torque, which is possible with a field oriented model. In this case, as was mentioned before, not only the structure of the control will be the same as the separately excited DC motor but we also get a similarly good dynamic control behaviour.

4. Motor Model Used in the Field Oriented Control

The model of the AC drive will be described in field coordinates⁴. As a basis, the equations of the motor as described in [4] will be used. This system of equations is nonlinear. The indices "R" and "S" mean rotor and stator respectively.

$$\underline{u}_S(t) = R_S \underline{i}_S(t) + \frac{d}{dt} \underline{\Psi}_S(t) = R_S \underline{i}_S(t) + L_S \frac{d}{dt} \underline{i}_S(t) + L_H \frac{d}{dt} (\underline{i}_R(t) e^{j\varepsilon(t)}) \quad (1)$$

$$0 = R_R \underline{i}_R(t) + \frac{d}{dt} \underline{\Psi}_R(t) = R_R \underline{i}_R(t) + L_R \frac{d}{dt} \underline{i}_R(t) + L_H \frac{d}{dt} (\underline{i}_S(t) e^{-j\varepsilon(t)}) \quad (2)$$

$$m_d(t) = \frac{2}{3} z_p L_H \text{Im}[\underline{i}_S(t) (\underline{i}_R(t) e^{j\varepsilon(t)})^*] \quad (3)$$

$$\frac{d\omega(t)}{dt} = \frac{z_p}{J} (m_d(t) - m_L(t)) \quad (4)$$

$$\frac{d\varepsilon(t)}{dt} = \omega(t) \quad (5)$$

The inductances in these equations are defined as:

$$L_S = L_{\sigma_S} + L_H = (1 + \sigma_S) L_H \quad L_R = L_{\sigma_R} + L_H = (1 + \sigma_R) L_H \quad (6)$$

The total leakage factor is defined as follows:

$$\sigma = 1 - \frac{L}{(1 + \sigma_S)(1 + \sigma_R)} \quad (7)$$

L_H is the main inductance of the motor, R_S and R_R are the resistances of the windings.

We will now define the model of the asynchronous motor in field coordinates. This will make it possible to implement the controller in field coordinates. Field orientation is described in detail in [1]. The basic principle is, that we convert all values to the coordinate system of the magnetic field, decompose the stator current vector into a field

⁴In none of these models of the Asynchronous Motor do we take the mechanical losses into account.

generating, and a torque generating (i_{sd} and i_{sq} respectively) component. Once this is done, the actual control becomes very simple. Since our program does not reach the field weakening range, we will keep the field generating component at a constant value to generate a necessary field, and control the torque generating component according to the speed. This means, that the output of the speed controller is the reference for the i_{sq} controller.

We will eliminate the use of flux in the model, and we will use the magnetizing current instead. The connection between these two variables is as follows:

$$\underline{i}_{mR}(t) = (1 + \sigma_R) \underline{i}_R(t) e^{j\epsilon(t)} + \underline{i}_S(t) = \underline{i}_{mR}(t) e^{j\rho(t)} = \frac{1}{L_H} \underline{\Psi}_R(t) e^{j\epsilon(t)} \quad (8)$$

The transformation between the systems will be done by the following transformation:

$$\underline{u}_S e^{-j\rho} = u_{sd} + j u_{sq} \quad (9)$$

$$\underline{i}_S e^{-j\rho} = i_{sd} + j i_{sq} \quad (10)$$

Let us now consider the equations of the model in field coordinate system. Note that in these equations $T_R = \frac{L_R}{R_R}$. Note also, that the rotor based variables are also completely eliminated.

$$u_{sd}(t) = R_S i_{sd}(t) + \sigma L_S \frac{d}{dt} i_{sd}(t) - \sigma L_S \omega_{mR}(t) i_{sq}(t) + (1 - \sigma) L_S \frac{d}{dt} i_{mR}(t) \quad (11)$$

$$u_{sq}(t) = R_S i_{sq}(t) + \sigma L_S \frac{d}{dt} i_{sq}(t) + \sigma L_S \omega_{mR}(t) i_{sd}(t) + (1 - \sigma) L_S \omega_{mR}(t) i_{mR}(t) \quad (12)$$

$$i_{sd}(t) = i_{mR}(t) + T_R \frac{d}{dt} i_{mR}(t) \quad (13)$$

$$i_{sq}(t) = (\omega_{mR}(t) - \omega(t)) T_R i_{mR}(t) \quad (14)$$

$$m_d(t) = \frac{2}{3} z_p (1 - \sigma) L_S i_{mR}(t) i_{sq}(t) \quad (15)$$

$$\frac{J}{z_p} \frac{d\omega(t)}{dt} = m_d(t) - m_L(t) \quad (16)$$

This model has been the basis for the field oriented control. Note, that the Kalman filter in the next section is based on another model, which uses rotor fluxes and stator currents as state variables. These two models are equivalent. The other model will be presented where the Kalman filter is introduced.

5. Implementation of the Field Oriented Control Method

Using the field oriented model of the motor, it has theoretically become possible to realize a control in field orientation, which makes it extremely easy to control speed by controlling i_{Sq} . However our system of equations is nonlinear. We will eliminate this non-linearity by a decoupling of the nonlinear terms. This method is taken from [4].

$$u_{Sd} = u_{Sd}^{Lin} + u_{Sd}^{Couple} = \left[R_S i_{Sd} + \sigma L_S \frac{d}{dt} i_{Sd} \right] + \left[-\sigma L_S \omega_{mR} i_{Sq} + (1 - \sigma) L_S \frac{d}{dt} i_{mR} \right] \quad (17)$$

$$u_{Sq} = u_{Sq}^{Lin} + u_{Sq}^{Couple} = \left[R_S i_{Sq} + \sigma L_S \frac{d}{dt} i_{Sq} \right] + \left[\sigma L_S \omega_{mR} i_{Sq} + (1 - \sigma) L_S \omega_{mR} i_{mR} \right] \quad (18)$$

From these equations we derive the formula for the linearized voltages, which will make our equations linear.

$$u_{Sd}^{Lin} = u_{Sd} - u_{Sd}^{Couple} = \left[R_S i_{Sd} + \sigma L_S \frac{d}{dt} i_{Sd} \right] \quad (19)$$

$$u_{Sq}^{Lin} = u_{Sq} - u_{Sq}^{Couple} = \left[R_S i_{Sq} + \sigma L_S \frac{d}{dt} i_{Sq} \right] \quad (20)$$

Now we will presume, that $i_{mR} = i_{mR}^{ref}$, and that it is constant. This will remove the last non linearity by making K_J constant.

$$\frac{d}{dt} \begin{bmatrix} i_{Sd} \\ i_{mR} \\ i_{Sq} \\ \omega \\ \varepsilon \end{bmatrix} = \begin{bmatrix} -\frac{R_S}{\sigma L_S} & 0 & 0 & 0 & 0 \\ \frac{1}{T_R} & -\frac{1}{T_R} & 0 & 0 & 0 \\ 0 & 0 & -\frac{R_S}{\sigma L_S} & 0 & 0 \\ 0 & 0 & K_J & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} i_{Sd} \\ i_{mR} \\ i_{Sq} \\ \omega \\ \varepsilon \end{bmatrix} + \begin{bmatrix} \frac{1}{\sigma L_S} & 0 & 0 \\ 0 & \frac{1}{\sigma L_S} & 0 \\ 0 & 0 & -\frac{z_p}{J} \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} u_{Sd}^{Lin} \\ u_{Sq}^{Lin} \\ m_L \end{bmatrix} \quad (21)$$

where

$$K_J = \frac{2}{3} \frac{z_p^2}{J} (1 - \sigma) L_S i_{mR}^{ref} \quad (22)$$

This system can be split into two systems, the d and the q subsystem. This will enable us to build up a separate controller for both parts. The d and the q subsystems are the following:

$$\frac{d}{dt} \begin{bmatrix} i_{sd} \\ i_{mR} \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{\sigma L_s} & 0 \\ \frac{1}{T_R} & -\frac{1}{T_R} \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{mR} \end{bmatrix} + \begin{bmatrix} 1 \\ \sigma L_s \\ 0 \end{bmatrix} u_{sd}^{Lin}; \quad y_q = \begin{bmatrix} 0 & 1 \end{bmatrix} \begin{bmatrix} i_{sq} \\ i_{mR} \end{bmatrix} \quad (23)$$

$$\frac{d}{dt} \begin{bmatrix} i_{sq} \\ \omega \\ \varepsilon \end{bmatrix} = \begin{bmatrix} -\frac{R_s}{\sigma L_s} & 0 & 0 \\ K_J & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} i_{sq} \\ \omega \\ \varepsilon \end{bmatrix} + \begin{bmatrix} \frac{1}{\sigma L_s} & 0 \\ 0 & -\frac{z_p}{J} \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u_{sq}^{Lin} \\ m_L \end{bmatrix}; \quad y_d = \begin{bmatrix} 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} i_{sq} \\ \omega \\ \varepsilon \end{bmatrix} \quad (24)$$

After this it is possible to control the motor, provided that we are able to convert all values to field coordinates. This is made by the flux model. The form of the flux model, which is realized here is based on [1] and [7].

After realizing the flux model it is possible to control. The first branch of the control looks like this: There is a controller for i_{mR} , which is in fact a controller for Ψ , the flux. There is a controller for i_{sd} , which will force the correct i_{mR} . The second branch begins with a controller for ω , which is in turn followed by a controller for i_{sq} , which will force the correct torque and will realize the correct velocity. The overall control structure is given in Figure 2, with the controllers shown in the upper left corner.

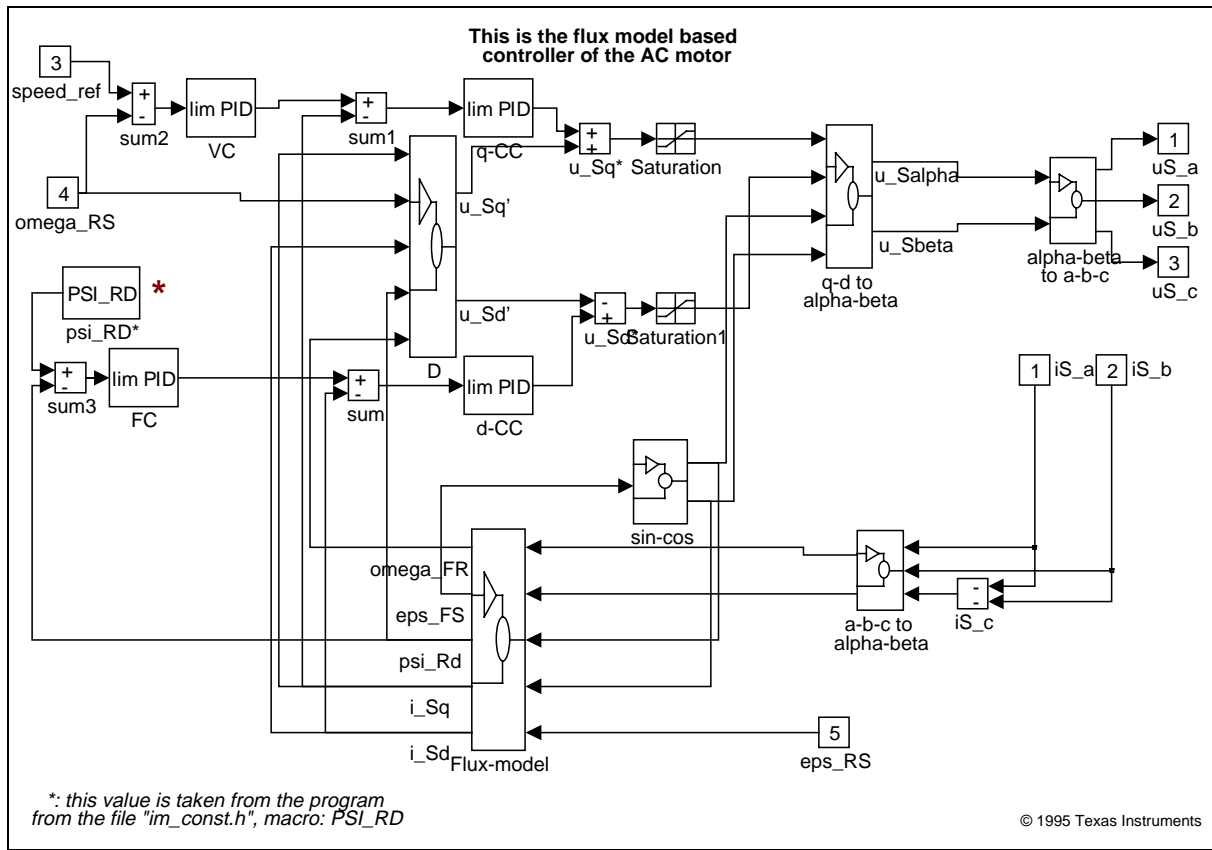


Figure 2: Model 1 - Field Oriented Controller for the ASM

The Field oriented control has been implemented as a simulation in Simulink, and also in real time on a C50 processor. A detailed documentation of this implementation can be found in [5].

6. Kalman Filter

The system we have considered up to now uses a sensor to measure position of the rotor. In many cases it is impossible to use sensors for speed measurement, perhaps because it is either technically impossible or extremely expensive. As an example, we can mention the pumps used in oil rigs to pump out the oil. These have to work under the surface of the sea, sometimes at depths of 50 meters, and getting the speed measurement data up to the surface means extra cables, which is extremely expensive. Cutting down the number of sensors and measurement cables provides a major cost reduction.

Lately, there have been many proposals addressing this problem, and it has turned out that speed can be calculated from the current and voltage values of the AC motor. Some of these proposals are open loop solutions, which give some estimation of speed, but these solutions normally have a large error. For better results we need an observer or a filter. The Kalman filter has a good dynamic behaviour, disturbance resistance, and it can work even in a standstill position. See [11] for a comparison of the performances of an observer, a Kalman filter (KF) and an Extended Kalman filter (EKF).

Implementing a filter is a very complex problem, and it requires the model of the AC motor to be calculated in real time. Also, the Filter equations must be calculated, which normally means many matrix multiplications and one matrix inversion. Nevertheless, these requirements can be fulfilled by a processor with high calculation performance. A DSP is especially well suited for this purpose, because of its good calculation-performance/price ratio. In low cost applications *fixed point* DSPs are desirable.

The chosen solution is a Kalman filter, which is a statistically optimal observer (see exact details in [2]), if the statistical characteristics of the various noise elements are known. For the implementation of the Kalman filter we need a much greater calculating capacity than the C14 used in [6] to realize the field oriented control, so the C50 DSP has been chosen. This makes things more complicated of course, since the variables have to be scaled, which would be unnecessary with a floating point processor.

For information on the hardware used in this project see [5].

At this point, the question of the portability has to be mentioned. The portability of this software is very limited, if we look at the processor side only. It is however a special purpose software for DSPs, so it makes sense to look at the portability only to other DSPs. The fixed point DSPs of Texas Instruments are upward source code compatible, which makes it easy to port the software to newer DSPs. Porting to older versions is also quite simple, the special C50 instructions must be substituted. The software is modular, so porting it to another hardware platform with the same processor but other peripherals only means substituting the I/O routines, and setting the parameters. So we can justly claim that the portability of the software inside the fixed point DSP family is very good.

First a short introduction to the theory of Kalman filters will be presented. This introduction will be based partly on [2], partly on [3].

The Kalman filter is a special kind of observer, which provides optimal filtering of the noises in measurement and inside the system if the covariance matrices of these noises are known. So let us first see what an observer is.

7. Basics of Observers

The problem of the observers is the following. Take a system which has some internal states: these state variables are normally not measurable so we usually measure only substitute variables. If we want to know these internal state variables for some reason, for example, we want to be able to control them, then we have to calculate them. It is not always possible to calculate these variables directly from the measured outputs.

Consider a system with the following form. (Note, that all symbols that denote matrices or vectors are underlined.)

$$\dot{\underline{x}} = \underline{A}\underline{x} + \underline{B}u \quad (25)$$

$$\underline{y} = \underline{C}\underline{x} \quad (26)$$

With a very simple approach we can realize a system, that runs parallel to the real system, and it calculates the state vector, as seen in Figure 3. This is based on the quite reasonable assumption, that we know the input values of the system.

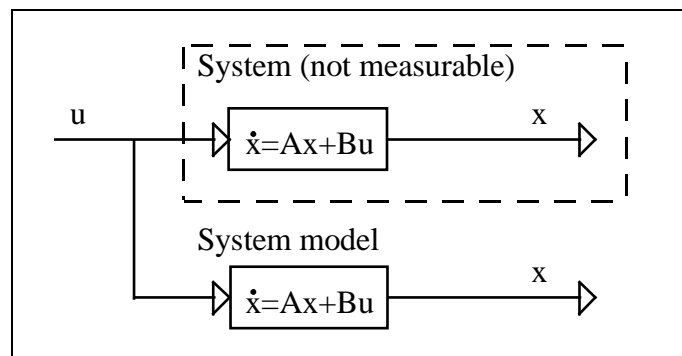


Figure 3: Reconstruction of the State Vector

This approach however does not take into account that the starting condition of the system is unknown, which is true in practically every case. This causes the state variable vector of the system model to be different from that of the real system.

The problem can be overcome by using the principle that the estimated output vector is calculated based on the estimated state vector,

$$\hat{\underline{y}} = \underline{C}\hat{\underline{x}} \quad (27)$$

which may then be compared with the measured output vector. The difference will be used to correct the state vector of the system model. This is called the Luenberger observer, and it can be seen in Figure 4.

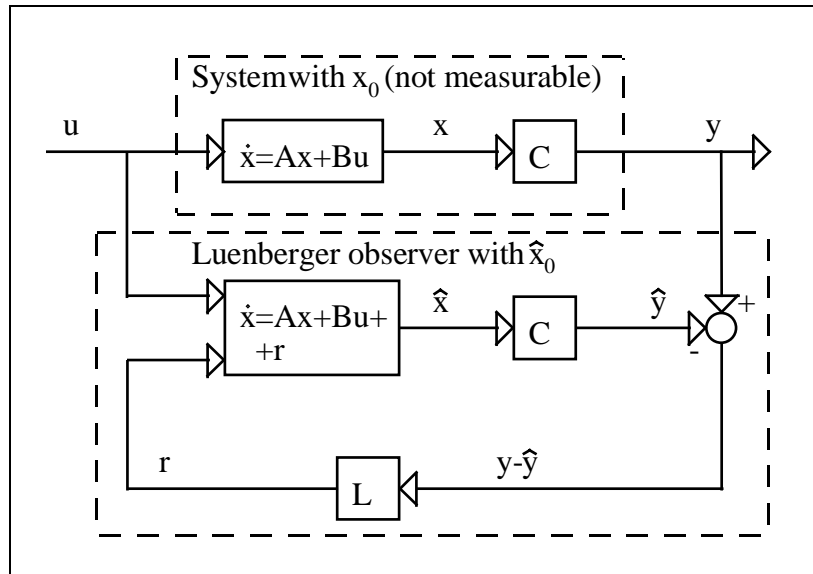


Figure 4: Structure of the Luenberger Observer

Now we can set up the state equation of the Luenberger Observer as the following:

$$\dot{\hat{x}} = (\underline{A} - \underline{L}\underline{C})\hat{x} + \underline{B}u + \underline{L}y \quad (28)$$

Now we can ask how the matrix L must be set in order to make the error go to zero. This is done by setting up a state equation for the error as follows:

$$\dot{\tilde{x}} = (\underline{A} - \underline{L}\underline{C})\tilde{x} \quad (29)$$

where:

$$\tilde{x} = x - \hat{x} \quad (30)$$

If we now transpose the matrix of the error differential equation (29), we get a form which is very similar to a controller structure:

$$\dot{x}_f = (\underline{A}^T - \underline{C}^T \underline{L}^T)x_f \quad (31)$$

The effectiveness of such an observer greatly depends on the exact setting of the parameters, and the exact measurement of the output vector. In the case of a real system, none of these criteria can be taken for granted. In the event of relatively great disturbances in the measurement, great parameter differences, or internal noises in the system, the Luenberger observer cannot work anymore and we have to turn to the Kalman filter.

8. Basics of Kalman Filters

The Kalman filter provides a solution that directly cares for the effects of the disturbance noises. The errors in the parameters will normally also be handled as noise. Let us assume a system with the following equations.

$$\dot{\underline{x}} = \underline{A}\underline{x} + \underline{B}\underline{u} + \underline{r} \quad (\text{System}) \quad (32)$$

$$\underline{y} = \underline{C}\underline{x} + \underline{\rho} \quad (\text{Measurement}) \quad (33)$$

Where \underline{r} and $\underline{\rho}$ are the system and the measurement noise. Now we assume, that these noises are stationary, white, uncorrelated and Gauss noises, and their expectation is 0. Let us now define the covariance matrices of these noises:

$$\text{cov}(\underline{r}) = E\{\underline{r}\underline{r}^T\} = \underline{Q} \quad (34)$$

$$\text{cov}(\underline{\rho}) = E\{\underline{\rho}\underline{\rho}^T\} = \underline{R} \quad (35)$$

Where $E\{\cdot\}$ denotes expected value.

The overall structure of the Kalman filter is the same as that of the Luenberger observer in Figure 4. The system equations are also the same:

$$\dot{\hat{\underline{x}}} = (\underline{A} - \underline{K}\underline{C})\hat{\underline{x}} + \underline{B}\underline{u} + \underline{K}\underline{y} \quad (36)$$

We will follow the notations of [2], and denote the matrix of the Kalman filter by \underline{K} . The only real difference between the Luenberger observer and the Kalman filter is the setting of the matrix \underline{K} . This will be done based on the covariance of the noises. We will first build the measure of the goodness of the observation, which is the following:

$$J = \sum_{i=1}^n E\{\tilde{x}_i^2\} \quad (37)$$

This depends on the choice of \underline{K} . \underline{K} has to be chosen to make J minimal. The solution of this is the following (see [11]):

$$\underline{K} = \underline{P}\underline{C}^T \underline{R}^{-1} \quad (38)$$

Where \underline{P} can be calculated from the solution of the following equation:

$$\underline{P}\underline{C}^T \underline{R}^{-1} \underline{C}\underline{P} - \underline{A}\underline{P} - \underline{P}\underline{A}^T - \underline{Q} = \underline{0} \quad (39)$$

\underline{Q} and \underline{R} have to be set up based on the stochastic properties of the corresponding noises. Since these are usually unknown they are used as weight matrices in most cases. They are often set equal to the unit matrix, avoiding the need of the deeper knowledge of noises.

In [2] a recursive algorithm is presented for the discrete time case to provide the solution for this equation. This algorithm is in fact the EKF (Extended Kalman Filter) algorithm, because the matrix of the Kalman filter, K , will be on-line calculated. The EKF is also capable of handling non-linear systems, such as the induction motor. In this case we do not have the optimum behaviour, which means the minimum variance, and it is also impossible to prove the convergence of the model. (See [11]).

Let us now see the recursive form of the EKF as in [9]. (This is basically the same as in [2], but with slightly different notation):

All symbols in the following formulas denote matrices or vectors. They are not denoted with a special notation, because there is no possibility of mixing them up with scalars.

$$x_{k|k} = x_{k|k-1} + K_k (y_k - h(x_{k|k-1}, k)) \quad (40)$$

$$P_{k|k} = P_{k|k-1} - K_k \left. \frac{\partial h}{\partial x} \right|_{x=x_{k|k-1}} P_{k|k-1} \quad (41)$$

$$K_k = P_{k|k-1} \left. \frac{\partial h^T}{\partial x} \right|_{x=x_{k|k-1}} \left(\left. \frac{\partial h}{\partial x} \right|_{x=x_{k|k-1}} P_{k|k-1} \left. \frac{\partial h^T}{\partial x} \right|_{x=x_{k|k-1}} + R \right)^{-1} \quad (42)$$

$$x_{k+l|k} = \Phi(k+l, k, x_{k|k-1}, u_k) \quad (43)$$

$$P_{k+1|k} = \left. \frac{\partial \Phi}{\partial x} \right|_{x=x_{k|k}} P_{k|k} \left. \frac{\partial \Phi^T}{\partial x} \right|_{x=x_{k|k}} + \Gamma_k Q \Gamma_k^T \quad (44)$$

Where

$$\Phi(k+l, k, x_{k|k-1}, u_k) = A_k(x_{k|k})x_{k|k} + B_k(x_{k|k})u_k \quad (45)$$

$$h(x_{k|k-1}, k) = C_k(x_{k|k-1})x_{k|k-1} \quad (46)$$

These are the system vector and the output vector respectively, and they can be explicitly calculated.

The matrix K is the feedback matrix of the EKF. This matrix determines how the state vector of the EKF is modified after the output of the model is compared with the real output of the system.

At this point it is important to mention that this system of equations contains many matrix operations, which can be difficult to implement in real-time.

To implement this recursive algorithm of course we will need the Model of the motor, which means the matrices A, B and C , from which we have to calculate the matrices Φ and h. So let us see the Motor Model.

9. Motor Model for the Kalman Filter

As shown in the previous section we need a model of the motor for the implementation of the KF. For this purpose two models have been tested, one of Brunsbach [9] and one of Vas [10]. The model of Vas has shown a more stable behaviour, and that is why we use it later for the implementation.

First, let us have a look at the model of [9].

$$\frac{d}{dt} \begin{bmatrix} i_{sd} \\ i_{mR} \\ i_{sq} \\ \omega \end{bmatrix} = \begin{bmatrix} \frac{1}{\sigma T_s} & \frac{1-\sigma}{\sigma} \frac{1}{T_R} & \frac{1-\sigma}{\sigma} \frac{1}{T_R} & \omega_{mR} & 0 \\ & \frac{1}{T_R} & -\frac{1}{T_R} & 0 & 0 \\ & -\omega_{mR} & -\frac{1-\sigma}{\sigma} \omega_{mR} T & -\frac{1}{\sigma T_s} & 0 \\ & 0 & 0 & \frac{2}{3} \frac{z_p^2}{J} (1-\sigma) L_s i_{mR} & 0 \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{mR} \\ i_{sq} \\ \omega \end{bmatrix} + \frac{1}{\sigma T_s R_s} \begin{bmatrix} \cos(\varepsilon) & \sin(\varepsilon) \\ 0 & 0 \\ -\sin(\varepsilon) & \cos(\varepsilon) \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u_{s\alpha} \\ u_{s\beta} \end{bmatrix} \quad (47)$$

$$\begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \\ \omega \end{bmatrix} = \begin{bmatrix} \cos(\varepsilon) & 0 & -\sin(\varepsilon) & 0 \\ \sin(\varepsilon) & 0 & \cos(\varepsilon) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} i_{sd} \\ i_{mR} \\ i_{sq} \\ \omega \end{bmatrix} \quad (48)$$

Note that in this model ω is part of the output vector. This does not mean that we measure it, but it must be estimated roughly and this estimated value must be substituted into the Kalman filter where this output vector is needed. The substitution is made based on the following formula:

$$\omega = \omega_{mR} - \frac{i_{sq}}{T_R i_{mR}} \quad (49)$$

This expression has to be calculated each time the model has to be evaluated. To evaluate this formula we need the speed of the flux, ω_{mR} . This means, that we require our flux model just as before. The flux model is also needed to calculate the angle of the flux, ε .

Now we will examine the other model proposed in [10].

$$\frac{d}{dt} \begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix} = \begin{bmatrix} -\frac{K_R}{K_L} & 0 & \frac{L_H R_R}{L_R^2 K_L} & \frac{L_H \omega}{L_R K_L} & 0 \\ 0 & -\frac{K_R}{K_L} & -\frac{L_H \omega}{L_R K_L} & \frac{L_H R_R}{L_R^2 K_L} & 0 \\ \frac{L_H}{T_R} & 0 & -\frac{1}{T_R} & -\omega & 0 \\ 0 & \frac{L_H}{T_R} & \omega & -\frac{1}{T_R} & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix} + \frac{1}{K_L} \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u_{s\alpha} \\ u_{s\beta} \end{bmatrix} \quad (50)$$

$$\begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{s\alpha} \\ i_{s\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix} \quad (51)$$

This model has a disadvantage; its order is higher. This will be a drawback when the EKF algorithm has to be implemented in real-time. One great advantage of this model, however, is that it does not assume that the speed is measured, so neither ω_{mR} nor ω has to be known. The other is that the flux model can be omitted, since this model also estimates the flux, and so the angle of the flux and any other parameters can be directly calculated. The model is also much simpler than the first one, since it does not contain conversions between the stator and the field coordinate system, and thus the nonlinear sine terms disappear from the input and output matrices.

In both cases we will need a discrete version of the systems. The conversion will be done by the following approximate formulas based on [9]:

$$A' = e^{AT} \approx I + AT \quad (52)$$

$$B' = \int_0^T e^{A\xi} B d\xi \approx BT \quad (53)$$

$$C' = C \quad (54)$$

Where we denoted the system matrix, the input and output matrices of the continuous system with A , B and C , and those of the discrete system with A' , B' and C' . We assumed that our sampling time is very short compared with the dynamics of the system. From now on we will use the model presented in [10], so let us see the discrete form of this model.

$$\begin{bmatrix} i_{S\alpha} \\ i_{S\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix}_{k+1} = \begin{bmatrix} 1 - T \frac{K_R}{K_L} & 0 & T \frac{L_H R_R}{L_R^2 K_L} & T \frac{L_H \omega}{L_R K_L} & 0 \\ 0 & 1 - T \frac{K_R}{K_L} & -T \frac{L_H \omega}{L_R K_L} & T \frac{L_H R_R}{L_R^2 K_L} & 0 \\ T \frac{L_H}{T_R} & 0 & 1 - T \frac{1}{T_R} & -T \omega & 0 \\ 0 & T \frac{L_H}{T_R} & T \omega & 1 - T \frac{1}{T_R} & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} i_{S\alpha} \\ i_{S\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix}_k + T \frac{1}{K_L} \begin{bmatrix} 1 & 0 \\ 0 & 1 \\ 0 & 0 \\ 0 & 0 \\ 0 & 0 \end{bmatrix} \begin{bmatrix} u_{S\alpha} \\ u_{S\beta} \end{bmatrix}_k \quad (55)$$

$$\begin{bmatrix} i_{S\alpha} \\ i_{S\beta} \end{bmatrix}_k = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix} \begin{bmatrix} i_{S\alpha} \\ i_{S\beta} \\ \Psi_{R\alpha} \\ \Psi_{R\beta} \\ \omega \end{bmatrix}_k \quad (56)$$

After this point we will only look at the second model because the delivered results were much more stable.

10. Simulation of the Kalman Filter

Now that we have the discrete form of the model, we can calculate the necessary matrices and vectors for the recursion. This will be the last step to enable both real-time implementation and simulation.

$$\Phi = \begin{bmatrix} (1 - T \frac{K_R}{K_L})i_{S\alpha} + T \frac{L_H R_R}{L_R^2 K_L} \Psi_{R\alpha} + T \frac{L_H \omega}{L_R K_L} \Psi_{R\beta} + T \frac{1}{K_L} u_{S\alpha} \\ (1 - T \frac{K_R}{K_L})i_{S\beta} - T \frac{L_H \omega}{L_R K_L} \Psi_{R\alpha} + T \frac{L_H R_R}{L_R^2 K_L} \Psi_{R\beta} + T \frac{1}{K_L} u_{S\beta} \\ T \frac{L_H}{T_R} i_{S\alpha} + (1 - T \frac{1}{T_R}) \Psi_{R\alpha} - T \omega \Psi_{R\beta} \\ T \frac{L_H}{T_R} i_{S\beta} + T \omega \Psi_{R\alpha} + (1 - T \frac{1}{T_R}) \Psi_{R\beta} \\ \omega \end{bmatrix} \quad (57)$$

$$h = Cx = \begin{bmatrix} i_{S\alpha} \\ i_{S\beta} \end{bmatrix} \quad (58)$$

$$\frac{\partial \Phi}{\partial x} = \begin{bmatrix} 1 - T \frac{K_R}{K_L} & 0 & T \frac{L_H R_R}{L_R^2 K_L} & T \frac{L_H \omega}{L_R K_L} & T \frac{L_H}{L_R K_L} \Psi_{R\beta} \\ 0 & 1 - T \frac{K_R}{K_L} & -T \frac{L_H \omega}{L_R K_L} & T \frac{L_H R_R}{L_R^2 K_L} & -T \frac{L_H}{L_R K_L} \Psi_{R\alpha} \\ T \frac{L_H}{T_R} & 0 & 1 - T \frac{1}{T_R} & T \omega & T \Psi_{R\beta} \\ 0 & T \frac{L_H}{T_R} & T \omega & 1 - T \frac{1}{T_R} & T \Psi_{R\alpha} \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \quad (59)$$

$$\frac{\partial h}{\partial x} = \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \end{bmatrix} \quad (60)$$

Reaching this point the realization of the model in Matlab/Simulink can begin. Realizing the complete Kalman filter as a Simulink model would have been a very complicated model, and it seemed easier to implement it simply as a Matlab language file. Another advantage of this is that the Matlab language file can be more easily converted into an assembly program. A subsystem has been inserted into the system that contains the Kalman filter, which is then bound into the model as an S-function.

The overall structure of the controller is not changed very much. See Figure 5: Model 2. The filter is in the subsystem called KF. Its output depends on which model we use. The picture shows the case of the EKF with the second motor model (from [10]). In this case,

the outputs of the system are all state variables, which is the rotor fluxes and stator currents and rotor speed. The inputs are measured rotor currents and rotor voltages. In the other case the output would be only rotor speed, but the estimated rotor speed would be needed as well, which would be calculated by a flux model.

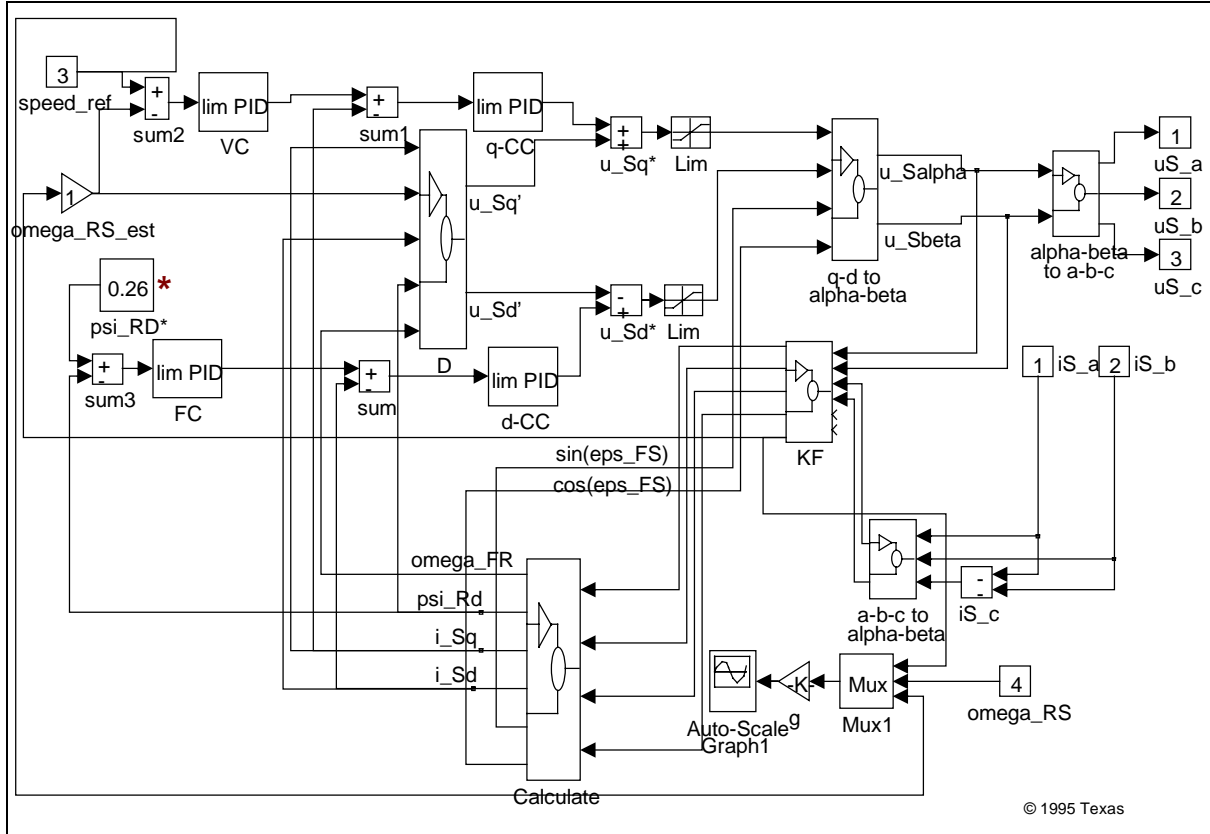


Figure 5: Model 2 - Controller with Kalman Filter

These tests reveal that the model of Vas (Presented in [10]) has a much more stable behaviour. In the Appendix the Extended Kalman Filter S-functions are presented for both motor models. For test results with the motor model please refer to the section "11 Simulation Results".

After achieving the required simulation results the real-time implementation could begin, again based on the second model.

11. Simulation Results

In this section the simulation results of the Field Oriented Control (FOC) and the EKF (Model of Vas) will be compared.

As a first test, let us compare the speed reversal of an FOC and an EKF. In both cases we apply a speed command of 2000RPM, and -2000RPM at 0.1 and 2.2s respectively. Also a constant load is applied at 1s in positive, and at 3s in negative direction.

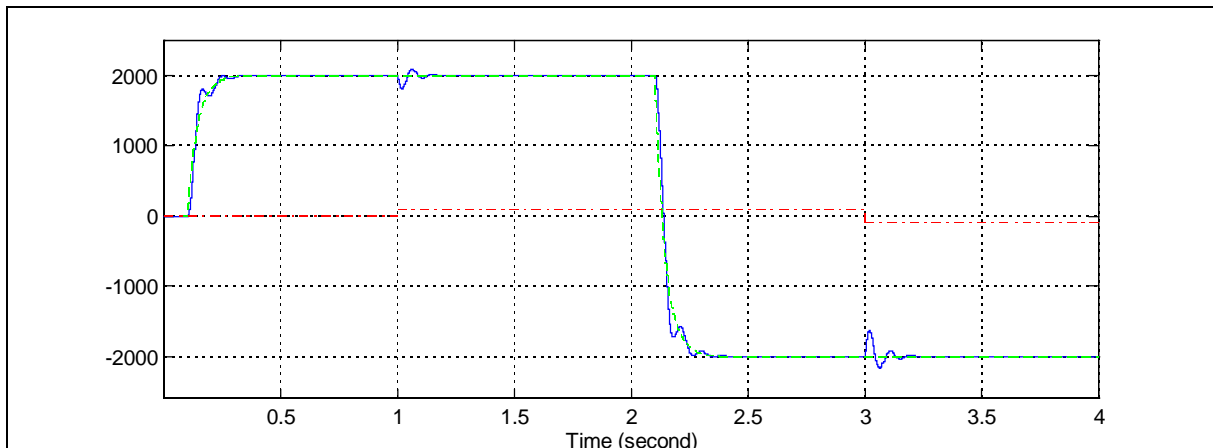


Figure 6: Speed Reversal with FOC

The figure shows the speed reference, speed and the load torque

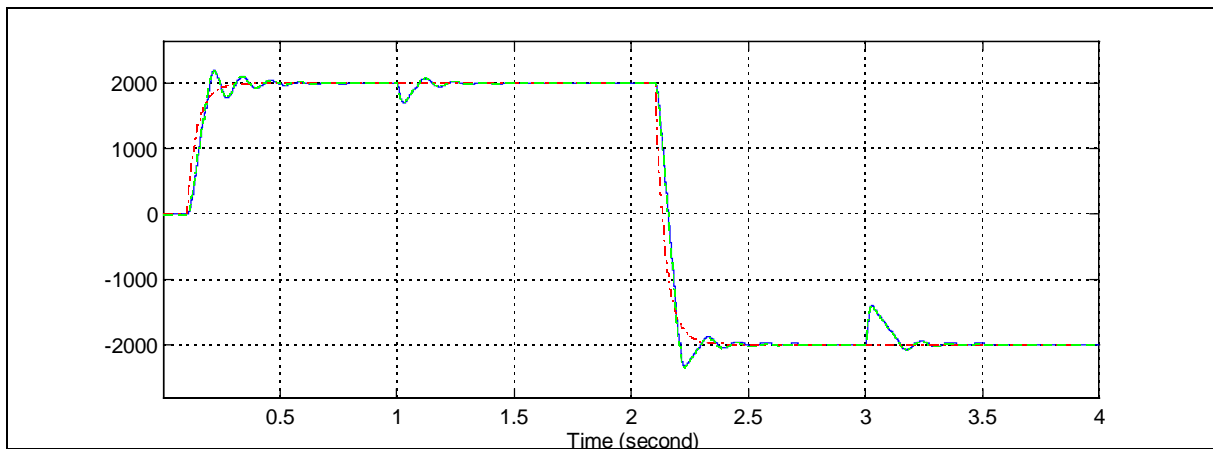


Figure 7: Speed Reversal with EKF

The figure shows the speed reference, estimated speed and the speed.

We can observe that the response of the EKF is worse than of the FOC, which is natural because we do not have an exact speed measurement, but the difference is not that great.

The next experiment shows load torque pulses applied to the motor in a standstill position. The torque is very large, so it causes very big changes in the speed. Let us first see, how the FOC behaves.

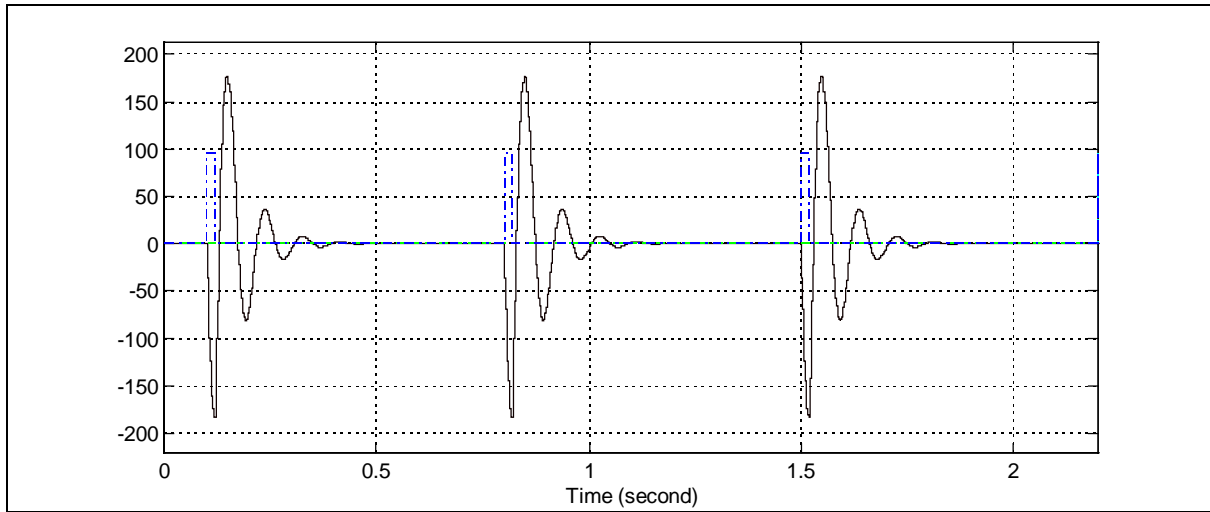


Figure 8: Applying Load at 0 RPM with FOC

The figure shows speed, torque and speed reference (always 0).

Let us now see the same test with the EKF.

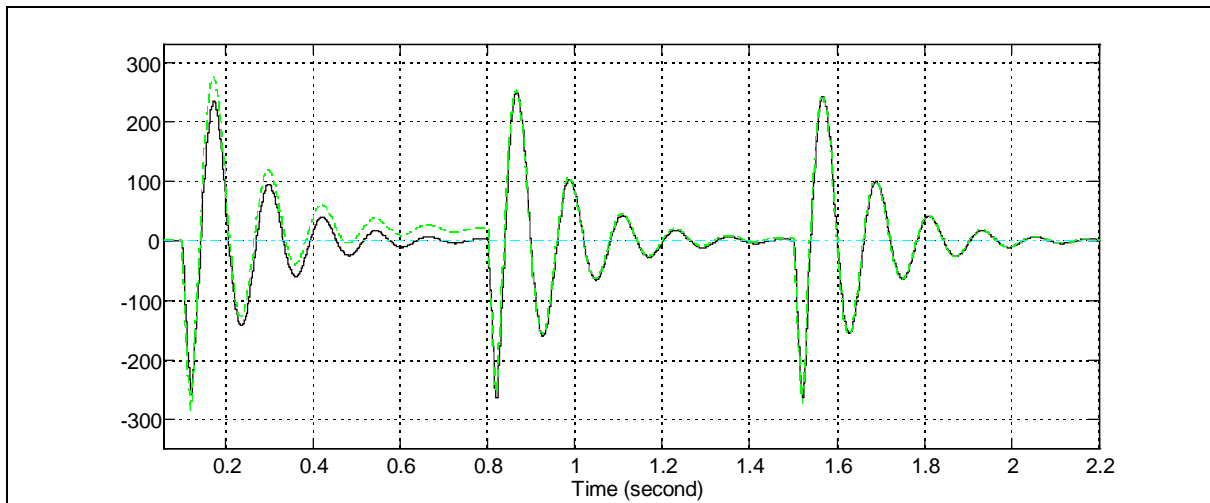


Figure 9: Applying Load at 0 RPM with EKF

It is clear that the offset gets very small after the second, and even smaller after the third, load impulse. This is due to the fact that the EKF parameters must settle before it can deliver good results and it needs some changes to be able to settle. This settling means that the K matrix reaches a point where it is more or less constant and its performance is close to optimal. Typical values of the K matrix after the first torque impulse:

$$K = \begin{matrix} & 0.1217 & -0.0245 \end{matrix}$$

```
-0.0245    0.0049
-0.0027    0.0005
 0.0005   -0.0001
 9.1643   -1.8304
```

This value leaves quite a big offset in the speed.

After the second torque impulse the offset will be very small, and K gets the following value:

```
K =
 0.0670    0.0632
 0.0632    0.0597
-0.0015   -0.0014
-0.0014   -0.0013
 6.8152    6.3945
```

This shows that there are great changes in K. As the system is nonlinear, we have to see that K will change all the time and will adapt the actual system conditions.

As a conclusion we can say that the simulation of the EKF shows a stable behaviour after a certain time has passed for settling. The torque disturbance rejection is very good, and comparable to the FOC. The simulations provide a basis for the real time implementation.

12. Real-Time Implementation of the Kalman Filter

In this chapter the real-time implementation using the TMS320C50 DSP will be presented.

The calculations look quite simple in the Matlab S-function, but we should not forget that all operations are matrix operations. Additionally there is a matrix inversion in the calculation process, which is very complex in the general case. These manipulations have to be ported to the assembly language of the C5x. Since the language has a very good macro support, these functions have been implemented with the help of macros.

To implement the matrix calculations, some matrix manipulation macros are needed. The most frequently needed was matrix multiplication. Let us see the matrix multiplication macro as an example.

```
; Matrix Multiplication Macro
;           Author :   Balazs Simor
;           Date   :   09. 1995.


---


; matrix multiplication for fractional matrices
; the macro does mat1*mat2=reslt.
; sizes of the matrices:
; mat1: [s11 x s21], mat2: [s21 x s22], reslt: [s11 x s22]
```

```

mmfra .macro mat1, mat2, reslt, s11, s21, s22
    setc ovm                ; saturation mode on.
    spm 1                   ; product shifted left by 1
    .asg 0,i
    .loop
    .asg 0,j
        .loop
            zap
            .asg 0,k
            .loop
                lta mat1+i*s21+k
                mpy mat2+k*s22+j
                .eval k+1,k
                .break(k == s21)
            .endloop
            apac
            sach reslt+s22*i+j
            .eval j+1,j
            .break(j == s22)
        .endloop
        .eval i+1,i
        .break (i == s11)
    .endloop
    clrc ovm                ; saturation mode off
    spm 0                   ; shifting off
    .endm

```

This macro implements a very general $[n \times m] \times [m \times l]$ matrix multiplication in a macro language. This has a great advantage, the cycles are generated and expanded by the compiler, and they do not take computation time. This macro relies basically upon the macro support of the Fixed Point DSP Assembler, for more information of the macro language see [13]. Note, this is a simplified version of the macro, but it shows the basic idea. For the complete macro see the Appendix.

The main reason why this function is implemented as a macro is that we need to multiply many different sized matrices. There is a list of the matrix multiplication operations needed in the following table. Since there are so many of these it did not make sense to implement each multiplication separately, and using loops would have made the calculations much slower. The macro language can handle the loops at compile time and achieve faster calculation.

Table 2: Some Types of Matrix Multiplication Needed For Kalman Filter

Matrix1 * Matrix2	Result
[5x5]*[5x5]	[5x5]
[2x5]*[5x5]	[2x5]
[2x5]*[5x2]	[2x2]
[5x2]*[2x2]	[5x2]
[5x5]*[5x2]	[5x2]
[5x2]*[2x1]	[5x1]
[5x2]*[2x5]	[5x5]

As an example for the speed of this macro we take a simple case of a [3x3]*[3x2] matrix multiplication. The macro will be expanded into 54 instructions, and the time needed for the execution will be 65 cycles. This is a measured value with the emulator. To see how to measure speed of programs with the TI tools, see [12] ("runb" debugger command).

Other matrix operations that are needed are: Inverting, Addition, Transposition, Vector normalization.

Inverting the matrix will be done by the Cramer rule:

$$A^{-1} = \frac{1}{\det(A)} \text{adj}(A) \quad (61)$$

Since we need the inverse of only a [2x2] matrix, the values can be explicitly calculated. Inverting has also been implemented in macros.

The macros available for inversion of a matrix are "madjG" for calculating the adjunct matrix, and "detG" for calculating the determinant of a matrix. To divide by the determinant, it is advisable to use the "mdsclG" macro. This macro divides a matrix by a scalar. Note, that the inverse of a matrix with elements in (-1,1) usually has elements out of this range. This means special care must be taken when calculating inverse.

The "mdsclG" macro makes a division of each element of a matrix by a scalar. This is usually a manipulation, where we lose a lot of accuracy, sometimes the complete result is incorrect. To overcome this problem, a "quasi floating point" division has been implemented. This means the scalar number is scaled so that its absolute value is in the range (0.5,1). Let us say that the scaling factor is 2^k . Then its "reciprocal" is calculated by dividing 0.5 by this scaled value, which is in fact $\frac{0.5}{2^k \text{ scl}}$ and in the range of (0.5,1), which means it is well scaled. The elements of the matrix are then calculated with this manipulated reciprocal and then left shifted by k+1. This method has the advantage that the "reciprocal" has the maximum accuracy achievable with 16 bits. The whole process can be expressed by the following formula:

$$\frac{a_{i,j}}{\text{scl}} = \frac{0.5}{2^k \text{ scl}} a_{i,j} 2^{k+1} \quad (62)$$

where scl is the scalar, and $a_{i,j}$ are the elements of the matrix.

This method can be called “quasi floating point”, because the reciprocal is in a form, where $\frac{0.5}{2^k scl}$ is its mantissa, and k+1 its exponent.

The addition and transposition are also realized in very simple macros. There are versions of these macros, that work with loops to make the need of program memory smaller.

There is a significant problem in storing the matrices. The macros can operate correctly only if the operand(s) and the result are on the same data page. We have quite a few matrices and a [5x5] matrix takes up as much as 25 words place. A data page has the size of 128 words, and we have 12 vectors and matrices of various sizes, which do not fit this page. The necessary space can be reduced if the transposed matrices are not calculated explicitly but a multiplication by transposed macro is created. This way diff_Fl transposed $(\frac{\partial \Phi^T}{\partial x})$, and diff_h transposed $(\frac{\partial h^T}{\partial x})$ do not have to be calculated. This also reduces the time needed for calculation. But the space taken up is still more than can fit on one page, so macros had to be created that can operate across pages. These macros use auxiliary registers of the DSP rather than direct addressing.

An interesting problem is normalizing vectors. This problem is encountered as the program has to calculate the transformation to field coordinates from the components of the rotor flux. The “vnormG” macro is available for this purpose. The macro works only with [2x1] vectors. The macro uses “quasi floating point” operations similar to the “mdsclG”. For this calculation the Newton-Raphson approximation of the square root is used, see [19] for short practical information.

Another important problem is that all the calculations have to be converted to fractional. This means that the ranges of the various parameters have to be known and scaled into the range of (-1,1). This is a difficult problem to handle in the case of the matrices which can have elements of very different ranges. Let us now see the scaling values for the various values in the matrices.

Table 3: Scaling Factors of Variables

Variable	Scaling Factor and Dimension
$i_{Sd}, i_{mR}, i_{Sq}, i_{\alpha}, i_{\beta}$	22.5 [A]
$\omega (= \omega_{RS}), \omega_{mR} (= \omega_{FS}), \omega_{FR}$ (electrical speed)	$2\pi \frac{n_{max}}{60} z_p \left[\frac{rad}{s} \right]_s$
ω_M, ω_{M-m} (mechanical speed)	$2\pi \frac{n_{max}}{60} \left[\frac{rad}{s} \right]$
$\varepsilon_{RS}, \varepsilon (= \varepsilon_{FS}), \varepsilon_{FR}, \varepsilon_M$	$\pi [rad]$
$u_{Sd}, u_{Sq}, u_{\alpha}, u_{\beta}$	155 [V]

The constants contained in the equations are presented in the following table.

Table 4: Constant Values

Constant	Value
T	500 μs
T_S	74.4 ms
T_R	40 ms
σ	0.084
R_S	1.68 Ω
L_S	0.125 H
J	0.00028 kg·m ²

Using these values the scaled vector Φ and the matrix $\frac{\partial \Phi}{\partial x}$ can be calculated. All the constants have to be pre-calculated to make the execution optimal. Here are these matrices:

$$\frac{\partial \Phi}{\partial x} = \begin{bmatrix} 0.6067 & 0 & 0.0562 & 0.7063\omega & 0.7063\Psi_{R\beta} \\ 0 & 0.6067 & -0.7063\omega & 0.0562 & -0.7063\Psi_{R\alpha} \\ 0.0559 & 0 & 0.9875 & -0.1571\omega & -0.1571\Psi_{R\beta} \\ 0 & 0.0559 & 0.1571\omega & 0.9875 & 0.1571\Psi_{R\alpha} \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix} \quad (63)$$

⁵With $n_{max} = 3000 \frac{I}{s}$ and $z_p = 2$.

We can see, that $\frac{\bar{\partial} \Phi}{\bar{\partial} x}$ is almost constant, and only 8 of its 25 elements have to be calculated each time. Since $\frac{\bar{\partial} \Phi}{\bar{\partial} x}$ contains the constants needed to calculate Φ , first $\frac{\bar{\partial} \Phi}{\bar{\partial} x}$ is calculated, and then Φ . This saves space since we have to reserve space for these constants only once - and also time, since products such as 0.7063ω have to be calculated only once in one recursion step.

13. Real Time Results

In this section the real-time results of the field oriented control and the EKF will be presented.

The program was tested with a method where all calculations have been compared with the formulas, thus checking the correctness of the implementation. After this, a 1 to 1 test has been made to compare the results with the ones without Kalman filter. The results were quite similar.

The results are quite similar to the ones like the simulated results. In this case also the standard test was used, the speed reversal test. Speeds mean electrical speed, so 1000 RPM corresponds to 500 RPM mechanical with a machine with two pole pairs ($p=2$).

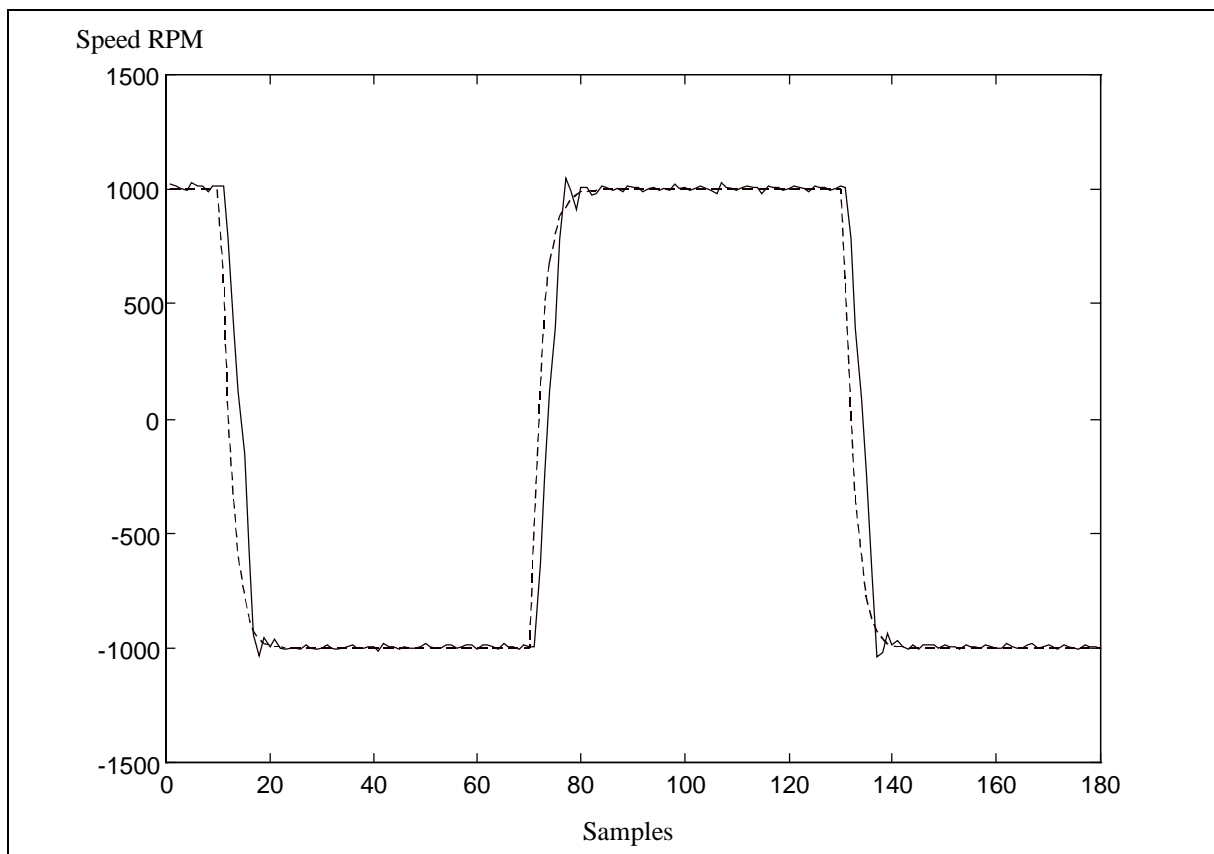


Figure 10: Speed Reversal with Kalman Filter

Note, the speed has a ripple on it, which shows that the behaviour should be improved. This may be achieved by tuning the Q and R covariance matrices. Another important factor is that the motor parameters have not been identified with the necessary tolerance, and much improvement can be expected here. Also note, this test, just as in case of the field oriented control, is without load torque.

As a comparison let us see the same experiment with the same controller settings with speed measurement.

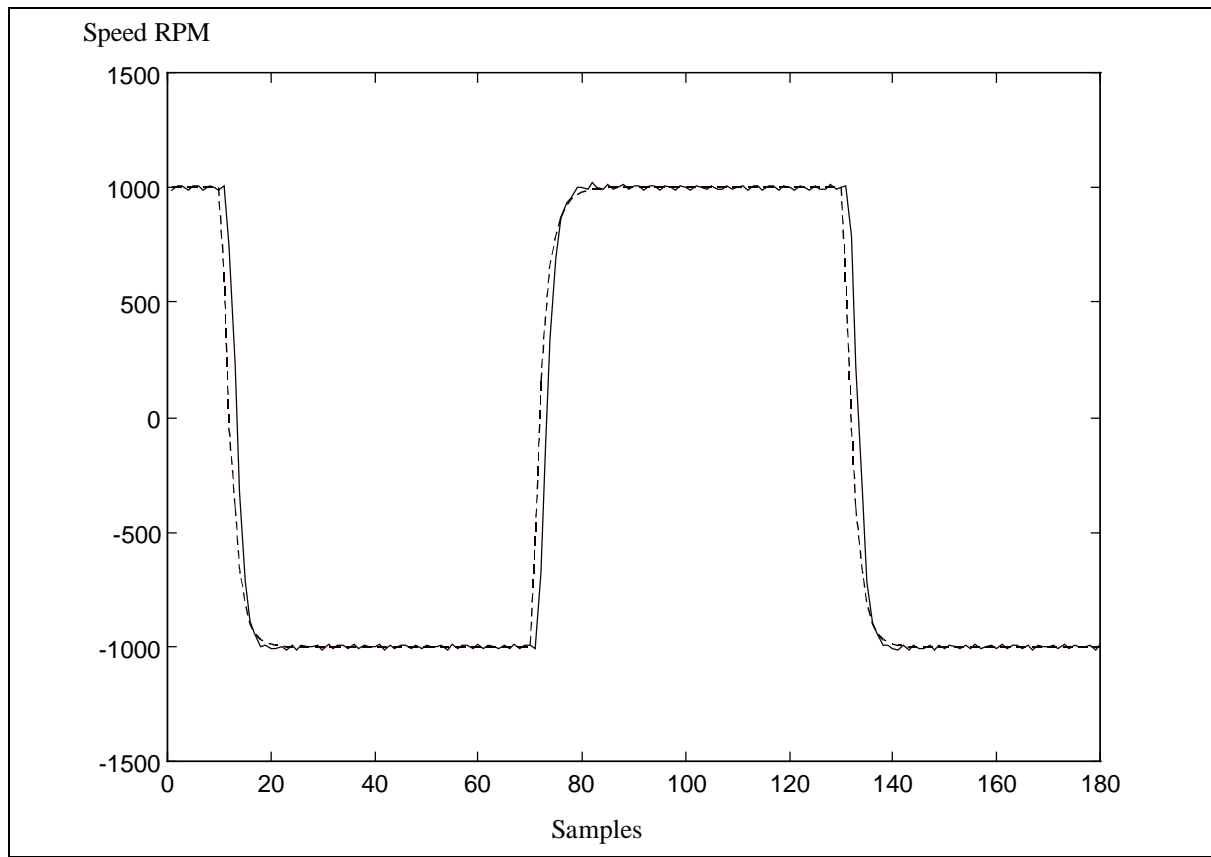


Figure 11: Speed Reversal with Speed Measurement

The program needs relatively little memory, the following table summarizes the needs:

Table 5: Memory Requirements of Kalman Filter

Program Part	Program Size (Words)	Data Size (Words)
Control+Kalman Filter	3641	631
Monitor Program	1577	603
Libraries	1605	309
Stack	0	1024
Σ Memory requirement	6823	2564

The Processor has a computing power of 20 MIPS at 20 MHz, which means a cycle time of 50 ns. The computation of the control happens in a 500 μ s cycle, so the processor has 10,000 cycles available. The processor is currently using about 4400-4700 cycles and this means that it has time to perform foreground tasks, such as Monitor programs, or

other communications. The processor computing capacity is used to about 50%, but the cycle times could also be reduced.

It should be mentioned here that further optimization in memory requirement and speed can be made by transferring more code directly to assembly language.

14. Conclusions and Possible Development

A model for the system has been prepared for comparison with the on-line results, and further development purposes. This model has been tested.

After that, the Kalman filter has been integrated to the simulation, in the form of a Matlab function, and it has been tested. The nonlinear Kalman filter algorithm based on [9] has been tested in the model. After the correct system model was chosen for the filter, the results were satisfactory.

An I/O library has been written to support the programming on board, which has then been extensively used in all software development.

The implementation of the Kalman filter has been done after this. Here the greatest problem was to keep the size of the program reasonable, and still reach a good performance. This was achieved by further optimizing the model with hand calculations to get a form of the EKF (Extended Kalman Filter) algorithm which can be implemented with relatively few instructions.

A further phase of the development could be fine tuning the Q and R matrices, which are the covariance matrices of the state and measurement noises and are used in the EKF. This fine tuning is usually done by experiments, see [11]. Another important improvement should be the possibility of exact identification of the system parameters.

There would be a need to convert this software partly into standard libraries. The libraries could provide the possibility to implement various control methods quickly, without low-level programming. It would be possible to overcome the slowness of C by using hand optimized assembly routines for frequent tasks, such as filtering or PID controllers. A library of fast and effective matrix manipulation in form of C callable functions or assembly macros would also be a very important step, which could be done enhancing the matrix manipulation macros in MATG.INC presented in the Appendix.

References

1. Leonhard: Control Of Electrical Drives, Springer-Verlag 1985
2. Brammer, Siffling: Kalman-Bucy Filter, Deterministische Beobachtung und stochastische Filterung. R. Oldenbourg Verlag Muenchen, Wien 1994.
3. Otto Föllinger: Regelungstechnik. Hüthig Buch Verlag GmbH Heidelberg, 1992.
4. Stefan Beierke: Vergleichende Untersuchungen von unterschiedlichen feldorientierten Lagereglerstrukturen fuer Asynchron-Servomotoren mit einem Multi-Transputer-System. Dissertation, Technische Universitaet Berlin 1992.
5. Balázs Simor: Design and Implementation of a Kalman Observer for an Induction Motor Based on a DSP System. Technical University of Budapest, 1995.
6. Dipl.-Ing. R. Neufeld, Dipl.-Ing. F.-J. Burs, Dr.-Ing. P.Krafka: Regelung einer Asynchronmaschine unter Verwendung des Signalprozessors TMS320E14, Universitaet Paderborn, 1993.
7. dSpace GmbH: Induction Motor Control with SIMULINK, dSpace, 1994 Preliminary Document Version 1.0
8. Dierk Schroeder, Clemens Schaeffner, Ulrich Lenz: Neural Net Based Observers for Sensorless Drives. IECON 1994, Volume 3.
9. B.-J. Brunsbach, G. Henneberger: Einsatz eines Kalman-Filters zum feldorientierten Betrieb einer Asynchronmaschine ohne mechanische Sensoren. Archiv fuer Elektrotechnik 1990 (Springer Verlag).
10. T. Du, P. Vas, A.F. Stronach, M.A. Brdys: Application of Kalman Filters and Extended Luenberger Observers in Induction Motor Drives. Intelligent Motion Proceedings, 1994.
11. C. Manes, F. Parasiliti, M. Tursini: Comparative Study of Rotor Flux Estimation in Induction Motors with a Nonlinear Observer and the Extended Kalman Filter. IECON 1994.
12. TMS320C5x C Source Debugger. User's Guide. Texas Instruments, 1991.
13. TMS320 Fixed-Point DSP Assembly Language Tools. User's Guide. Texas Instruments, 1991.
14. TMS320C2x/C5x Optimizing C Compiler. User's Guide. Texas Instruments, 1991.
15. TMS320C5x User's Guide. Texas Instruments, 1991.
16. SIMULINK (V1.3c). User's Guide. The Math Works, Inc. 1993.
17. MATLAB (V4.2c1). User's Guide. The Math Works, Inc. 1993.
18. Linear Circuits. Data Book Volume 2, Texas Instruments, 1992.
19. TMS320C5x User's Guide. Texas Instruments, 1995.



Appendix Source Code of Programs

Extended Kalman Filter in MATLAB Language

```
; Extended Kalman Filter as a Simulink S-function  
; Author : Balazs Simor  
; Date : November, 1995
```

```
function [sys, x0] = kalfil(t,x,u,flag, T)  
%kalman filter as an S-function (m-file)  
global Tr Ts Lr Ls Lh Kl Kr Rs Rr p J GAM Q R;  
global sig sigs out;  
global Tr_K Ts_K Lr_K Ls_K Lh_K Kl_K Kr_K Rs_K Rr_K p_K J_K;  
global sig_K sigs_K;  
global x_1 P_1 K P h FI Y omrs epsmr epsmr1 ommr co ommrfil isq omrsest;  
if flag == 0  
    kalini5  
    x0 = zeros(5,1);  
    sys = [0, 5, 5, 6, 0, 0];  
elseif flag == 2  
    % calc. inp and out vec of kalman filter  
    U = [u(1); u(2)];  
    Y = [u(3); u(4)];  
    %prediction  
    diff_FI=[1-Kr_K/Kl_K*T, 0, Lh_K*Rr_K/Lr_K/Lr_K/Kl_K*T, Lh_K/Lr_K*x(5)/Kl_K*T,  
Lh_K/Lr_K*x(4)/Kl_K*T;  
    0, 1-Kr_K/Kl_K*T, -Lh_K/Lr_K*x(5)/Kl_K*T, Lh_K*Rr_K/Lr_K/Lr_K/Kl_K*T,-  
Lh_K/Lr_K*x(3)/Kl_K*T;  
    Lh_K/Tr_K*T, 0, 1-T/Tr_K, -x(5)*T, -x(4)*T;  
    0, Lh_K/Tr_K*T, x(5)*T, 1-T/Tr_K, x(3)*T;  
    0, 0, 0, 0, 1];  
    x_1=[diff_FI(1,1)*x(1)+diff_FI(1,3)*x(3)+diff_FI(1,4)*x(4);  
    diff_FI(2,2)*x(2)+diff_FI(2,3)*x(3)+diff_FI(2,4)*x(4);  
    diff_FI(3,1)*x(1)+diff_FI(3,3)*x(3)+diff_FI(3,4)*x(4);  
    diff_FI(4,2)*x(2)+diff_FI(4,3)*x(3)+diff_FI(4,4)*x(4);  
    diff_FI(5,5)*x(5)]...  
    +T*[u(1)/Kl_K; u(2)/Kl_K; 0; 0; 0];  
    P_1=diff_FI*P*diff_FI' + GAM*Q*GAM'; %P[k|k-1] is ready  
    % calculation of h, diff_h  
    h=[x(1); x(2)];  
    diff_h=[1 0 0 0 0  
    0 1 0 0 0];
```

```
% system of Kalman filter
K=P_1*diff_h* inv(diff_h*P_1*diff_h' +R); %K[k]
out = x_1+K*(Y-h);    %x[k] is ready
sys = out;
P=P_1-K*diff_h*P_1;    %P[k] is ready
elseif flag == 3
    sys = out;
elseif flag == 4
    sys = (round(t/T)+1)*T;
else
    sys =[];
end
```

Full Source Code of Motor Control with EKF for C50

; Kalman Filter for the TMS320C5x

; Makefile

; Author : Balazs Simor

; Date : June, 1996

kalman.out : vel_ctr.obj ctr.obj sin.obj
 dsplnk \$** link.cmd -o \$@ -m map

matp.out : matp.obj
 dsplnk \$** link.cmd -o \$@ -m map

.c.asm :
 dspcl -O -g -n \$*

.asm.obj :
 dsps -l -v50 \$*

; Kalman Filter for the TMS320C5x

; matg.inc

; Author : Balazs Simor

; Date : June, 1996

; Matrix operation macros for C5x with Global mem access (With auxilliary
; registers of the processor)

; 1995 Balazs Simor

.mmregs

;matrix multiplication for fractional matrices

; the macro does mat1*mat2=reslt.

; reslt must not be mat1 or mat2.

; sizes: mat1: [s11 x s21], mat2: [s21 x s22], reslt: [s11 x s22]

mmfraG .macro mat1, mat2, reslt, s11, s21, s22

setc ovm ; saturation mode on.

spm 1 ;product shifted left by 1

lar AR0,#s22

mar *,AR2

.if (s21 >= 3)

.asg 0,i

.loop

.asg 0,j

.loop

lar AR2, #mat1+i*s21+0

lar AR3, #mat2+0*s22+j

lt *,AR3

mpy *0+,AR2

ltp *,AR3

mpy *0+,AR2

;lt mat1+i*s21+0

;mpy mat2+0*s22+j

;ltp mat1+i*s21+1

;mpy mat2+1*s22+j

.asg 2,k

.loop

lta *,AR3

mpy *0+,AR2

;lta mat1+i*s21+k

;mpy mat2+k*s22+j

.eval k+1,k

.break(k == s21)

```

        .endloop
        apac
        lar  AR2,#reslt+s22*i+j
        add  #16384,1
        sach *
        .eval j+1,j
        .break(j == s22)
    .endloop
    .eval i+1,i
    .break (i == s11)
.endloop
.else
.asg  0,i
.loop
    .asg  0,j
    .loop
        zap
        lar  AR2, #mat1+i*s21+0
        lar  AR3, #mat2+0*s22+j
        .asg 0,k
        .loop
            lta *+,AR3
            mpy *0+,AR2
            .eval k+1,k
            .break(k == s21)
        .endloop
        apac
        lar  AR2,#reslt+s22*i+j
        add  #16384,1
        sach *
        .eval j+1,j
        .break(j == s22)
    .endloop
    .eval i+1,i
    .break (i == s11)
.endloop
.endif
clrc ovm      ; saturation mode off
spm 0        ;shifting off
.endm

```

;matrix multiplication for fractional matrices with transposition

```

; the macro does mat1*mat2'=reslt.
; reslt must not be mat1 or mat2.
; sizes: mat1: [s11 x s21], mat2: [s22 x s21], reslt: [s11 x s22]
mmtfraG .macro mat1, mat2, reslt, s11, s21, s22
    setc ovm      ; saturation mode on.
    spm 1        ;product shifted left by 1
    mar *,AR2
    .if (s21 >= 3)
    .asg 0,i
    .loop
        .asg 0,j
        .loop
            lar AR2,#mat1+i*s21+0
            lar AR3,#mat2+j*s21+0
            lt  *+,AR3
            mpy *+,AR2
            ltp *+,AR3
            mpy *+,AR2
            ;lt mat1+i*s21+0
            ;mpy mat2+j*s22+0
            ;ltp mat1+i*s21+1
            ;mpy mat2+j*s22+1
            .asg 2,k
            .loop
                lta *+,AR3
                mpy *+,AR2
                ;lta mat1+i*s21+k
                ;mpy mat2+j*s22+k
                .eval k+1,k
                .break(k == s21)
            .endloop
        apac
        lar AR2,#reslt+s22*i+j
        add #16384,1
        sach *
        .eval j+1,j
        .break(j == s22)
    .endloop
    .eval i+1,i
    .break (i == s11)
    .endloop
    .else
    .asg 0,i

```

```

.loop
  .asg    0,j
  .loop
    zap
    lar AR2,#mat1+i*s21
    lar AR3,#mat2+j*s21
    .asg 0,k
    .loop
      lta *+, AR3
      mpy *+, AR2
      ;lta mat1+i*s21+k
      ;mpy mat2+j*s22+k
      .eval k+1,k
      .break(k == s21)
    .endloop
    apac
    lar AR2, #reslt+s22*i+j
    add  #16384,1
    sach *
    .eval j+1,j
    .break(j == s22)
  .endloop
  .eval i+1,i
  .break (i == s11)
.endloop
.endif
clrc ovm    ; saturation mode off
spm 0      ;shifting off
.endm

```

; matrix determinant for 2x2 matrices.
; input is fractional matrix, output is fractional

```

detG .macro mat, reslt
  setc ovm    ; saturation mode on
  spm 1      ; product sh mode 1
  lar  AR2, #mat
  lar  AR3, #mat+3
  mar  *,AR2
  lt   *+,AR3 ;a
  mpy  *-,AR2 ;d
  ltp  *,AR3 ;b

```

```

mpy  *,AR2  ;c

spac      ;ad-bc
lar  AR2,#reslt
add  #16384,1
sach  *
clrc  ovm  ; saturation mode off
spm  0  ; product sh mode 0
.endm

```

```

;matrix adjunct for 2x2 fractional matrices
; reslt must not be mat.

```

```

madjG .macro mat, reslt
    setc  ovm  ; saturation mode on
    spm  1  ; product sh mode 1

    lar  AR2, #mat
    lar  AR3, #reslt+3
    mar  *,AR2
    lacc  *+,AR3 ;a
    sacl  *,AR2
    lacc  *+,AR3 ;b
    sbrk  2
    neg
    sacl  *+,AR2
    lacc  *+,AR3 ;c
    neg
    sacl  *,AR2
    lacc  *, AR3 ;d
    sbrk  2
    sacl  *,AR2

    clrc  ovm  ; saturation mode off
    spm  0  ; product sh mode 0
.endm

```

```

;matrix addition
; reslt = mat1 + mat2
; reslt can be mat1, or mat2 as well.
maddG .macro mat1, mat2, reslt, s0, s1
    setc  ovm
    lar  AR2, #mat1

```

```

lar  AR3, #mat2
lar  AR4, #reslt
mar  *,AR2
.asg 0,i
.loop
    lacc  *+,16,AR3
    add  *+,16,AR4
    sach  *+,AR2
    .eval i+1, i
    .break(i == s0*s1)
.endloop
clrc  ovm
.endm

```

```

;matrix subtraction
; reslt = mat1-mat2;
; reslt can be mat1, or mat2 as well.
msubG .macro mat1, mat2, reslt, s0, s1

```

```

    setc  ovm
    lar  AR2, #mat1
    lar  AR3, #mat2
    lar  AR4, #reslt
    mar  *,AR2
    .asg 0,i
    .loop
        lacc  *+,16,AR3
        sub  *+,16,AR4
        sach  *+,AR2
        .eval i+1, i
        .break(i == s0*s1)
    .endloop
    clrc  ovm
    .endm

```

```

;matrix addition with diagonal matrix
; mat1 = mat1 + mat2
; where mat2 is a diagonal matrix, and it is stored as a vector.
madiG .macro mat1, mat2, s0

```

```

setc  ovm
lar   AR2, #mat1
lar   AR3, #mat2
lar   AR0, #s0+1
mar   *,AR2

```

```

.asg 0,i
.loop
  lacc *,16,AR3
  add  *,16,AR2
  sach *0+
  .eval i+1, i
  .break(i == s0)
.endloop
clrc  ovm
.endm

```

;matrix multiplied by a scalar (fractional)

; reslt = mat*scl;

; reslt can be mat as well

mmsclG .macro mat, scl, reslt, s0, s1

```

setc  ovm
spm   1
lar   AR2, #scl
mar   *,AR2
lt    *
lar   AR2, #mat
lar   AR3, #reslt
.asg 0,i
.loop
  mpy  *,+,AR3
  pac
  add  #16384,1
  sach *,+,AR2
  .eval i+1, i
  .break(i == s0*s1)
.endloop
clrc  ovm
spm   0
.endm

```

```

; matrix divided by a scalar. (Quasi Floating Point division)
; reslt = mat/scl;
; reslt and mat are [s0 x s1], scl is scalar
; t0 and t1 are temporary variables
mdsclG .macro mat, scl, reslt, s0, s1, t1

```

```

    lar  AR4,#0ffffh

```

```

    lar  AR2,#scl
    mar  *,AR2
    lacc *, 16, AR4
    bcnd epi?, eq      ;scl must not be 0!
    bcnd neg?, lt

```

```

x?

```

```

    sfl
    mar  *+          ;counting exponent in AR4
    bcnd x?,geq

```

```

    ror          ; rolling back to previous

```

```

    lar  AR2,#t1
    mar  *,AR2
    sach *
    lacc *          ;elimination of t1==16384
    sub  #16384
    bcnd ok?, NEQ
    lacc #16385
    sacl *

```

```

ok?

```

```

    lacc #16384,15
    rpt  #15
    subc *
    and  #0ffffh

```

```

    b    conti?

```

```

neg? neg

```

```

    mar  *,AR4

```

```

x1?

```

```

    sfl
    mar  *+
    bcnd x1?,geq

```

```

ror
lar  AR2,#t1
mar  *,AR2
sach *
lacc *          ;elimination of t1==16384
sub  #16384
bcnd ok?, NEQ
lacc #16385
sac1 *
ok1?
lacc #16384,15
rpt  #15
subc *
and  #0ffffh
neg

```

conti?

```

sac1 *
setc ovm
spm  1
lt   *
sar  AR4,*, AR3
lar  AR3,#mat
.asg 0,i
.loop
  mpy *+,AR2
  pac
  lar  AR4, *, AR4
loop:i:?          ; left shifting with saturation.
  sacb
  addb
  banz  loop:i:?

  ldp  #reslt+i
  add  #16384,1
  sach reslt+i
  mar  *,AR3
  .eval i+1, i
  .break(i == s0*s1)
.endloop

```

epi?

```

clrc  ovm
spm   0
.endm

```

```

; Vector normalization.

```

```

; reslt = vec/abs(vec);

```

```

; reslt and vec are [2 x 1] vectors

```

```

; t1 is a temporary store cell

```

```

vnormG .macro vec, reslt, t1

```

```

    lar  AR2, #vec

```

```

    lar  AR3, #reslt

```

```

    lar  AR4, #0

```

```

    lar  AR5, #t1 ;AR5->temp

```

```

    mar  *,AR2

```

```

    spm  0

```

```

    zap

```

```

    sqra  *+

```

```

    sqra  *-,AR4

```

```

    apac          ;ACCH= (abs(vec))^2/2

```

```

    rpt  #15

```

```

    norm  *+

```

```

    nop          ;pipeline protection

```

```

    nop

```

```

    mar  *,AR3

```

```

    sach  *+          ;Store normalized value of (abs(vec))^2/2 in reslt

```

```

    splk  #27969, *-   ;Beginning value for the iteration

```

```

.loop  3

```

```

    lt  *+          ;N/2

```

```

    mpy  *,AR5      ;R[i-1]

```

```

    pac

```

```

    sach  *,1

```

```

    lt  *,AR3      ;T=N/2*R[i-1]

```

```

    mpy  *,AR5      ;R[i-1]

```

```

    pac

```

```

    neg

```

```

    add  #32767,15

```

```

    add  #16385,15  ;ACCH=(1.5-(N/2)*R[i-1]^2)>>>1

```

```

sach *
lt *,AR3
mpy * ;R[i-1]
pac
sach *-,2 ;Storing new R[i]
.endloop

```

```

mar *+
lt *-,AR2 ;T=1/Root
mpy *+,AR3
pac
sach *+,1,AR2
mpy *,AR3
pac
sach *-,1,AR5

```

;denorming the values

```

sar AR4,*
lacc *
bcnd nodenorm1?,EQ ;no denorming if shiftcount is 0
ror
sac1 *
lar AR4*,AR4
mar *- ;decrementing AR4 for looping
bcnd even?,NC
mar *+, AR3 ;if odd, it must be incremented
lt *
mpy #23170 ;sqrt(2)/2
pac
sach *+,1
lt *
mpy #23170 ;sqrt(2)/2
pac
sach *-,1

```

even?

```
mar *,AR3
```

loop?

```

lacc *,16
add *,16
sach *+
lacc *,16

```

```
add    *,16
sach   *-,AR4
banz   loop?,AR3
```

```
nodenorm1?
```

```
.endm
```

```
; Kalman Filter for the TMS320C5x
; ctr.asm
; Author : Balazs Simor
; Date : June, 1996
```

```
cls_lp .set 1 ;1 if kalman filter is in the closed loop,
;0 for open loop
```

```
;-----Globals-----
```

```
;---Functions---
```

```
.globl _sine
.globl _c_int0
.globl _c_int4
.globl timer
.globl _get_incr ;incremental encoder IF
.globl _send_to_pwm
```

```
;---Variables---
```

```
.globl _i_sq_max
.globl _i_sd_ref
.globl _omega_m_ref
.globl _omega_m_ref_delayed
.globl _u_a
.globl _u_b
.globl _u_c
.globl _i_sd
.globl _d_decouple
.globl _phase_current
.globl _i_sd_m
.globl _omega_fr
.globl _omega_m
.globl _omega_m_est
.globl _omega_m_m
.globl _eps_m
.globl _eps_m_est
.globl _i_sq_m
.globl _psi_rd
.globl _x_psi
.globl _eps_fs
.globl _omega_fs
.globl _omega_rs
.globl _i_sq_scal
```

```

.globl _i_sd
.globl _d_decouple
.globl _i_sq_ref
.globl _i_sq
.globl _q_decouple
.globl _psi_decouple
.globl _u_a
.globl _u_b
.globl _u_c
.globl _u_a_mod
.globl _u_b_mod
.globl _u_c_mod
.globl _u_sd
.globl _u_sq

.globl _x
.globl _x_1
.globl _K

.globl _pwm_period_reg
.globl _pwmon

```

```

;-----Base Addresses-----

```

```

MODIFIED .set 0 ; modified address lines on the board

```

```

*****

```

```

*Register addresses of the PWM UNIT.

```

```

.if MODIFIED=1

```

```

PWMTCR .set 1000H

```

```

PWMTR .set 1001h

```

```

PWMPR .set 1008h

```

```

PWMCR0 .set 1009h

```

```

PWMCR1 .set 1002h

```

```

PWMCR2 .set 1003h

```

```

PWMAR .set 100ah

```

```

PWMIR .set 100bh

```

```

PWMVR .set 1004h

```

```

PWMDTR .set 1005h

```

```

PWMIOR .set 100ch

```

```

.else

```

```

PWMTCR .set 1000H

```

```

PWMTR .set 1001h

```

```

PWMPR .set 1002h

```

```

PWMCR0 .set 1003h

```

```

PWMCR1 .set 1004h
PWMCR2 .set 1005h
PWMAR .set 1006h
PWMIR .set 1007h
PWMVR .set 1008h
PWMDTR .set 1009h
PwMIOR .set 100ah
    .endif

```

```

*****

```

```

*Register addresses of the GPIO UNIT.

```

```

    .if MODIFIED=1
GPIOTCR .set 0000H
GPIOTR .set 0001h
GPIOPR .set 0008h
GPIOCCR .set 0009h
GPIOCR0 .set 0002h
GPIOCR1 .set 0003h
GPIOCR2 .set 000ah
GPIOCR3 .set 000bh
GPIOCOR .set 0004h
GPIOIO .set 0005h
GPIOCRIO .set 000ch
GPIOCRIO1 .set 000dh
GPIOIT .set 0006h
GPIOVEC .set 0007h
GPIOCMP .set 000eh
    .else
GPIOTCR .set 0000H
GPIOTR .set 0001h
GPIOPR .set 0002h
GPIOCCR .set 0003h
GPIOCR0 .set 0004h
GPIOCR1 .set 0005h
GPIOCR2 .set 0006h
GPIOCR3 .set 0007h
GPIOCOR .set 0008h
GPIOIO .set 0009h
GPIOCRIO .set 000ah
GPIOCRIO1 .set 000bh
GPIOIT .set 000ch
GPIOVEC .set 000dh
GPIOCMP .set 000eh
GPIOINC .set 000fh

```

```

        .endif
*****
*Addresses of ADC and MUX
ADBASE .set 2000h
MUXBASE .set 2001h

;-----Reset Vectors-----
        .sect "vectors"    ;power up reset vector
        b    _c_int0      ;go to start of program
        .space 16*6
        b    _c_int4      ;timer interrupt

        .data
        .align

variables:
counter .word 0 ;variable for switching between
;-----Cur. Control-----
cur_control:    ;/* here are all variables for the current control*/
temp .word 0
temp1 .word 0
temp2 .word 0
_pwm_period_reg .word 0

; /*From ACCTRL.H */
;-- system matrices of current controllers
;-- i_a not necessary --> high precision mode
;i_b : scalable constant vector (4) of fractional
; := ( 1.35898572914201E-01,
;     -1.35898572914201E-01,
;     0.00000000000000E+00,
;     0.00000000000000E+00);
;i_b .int 4453, -4453, 0, 0 ;Not scaled
;MODIFIED FOR NEW TIMING
_i_b .int 4453*2, -4453*2, 0, 0 ;Not scaled

;i_c : scalable constant vector (1) of fractional
; := ( 1.00000000000000E+00);
_i_c .int 4096 ;Scaled by 2^-3

```

```

;i_d : scalable constant vector (4) of fractional
; := ( 2.36686390532544E+00,
;    -2.36686390532544E+00,
;    7.14981873603059E-01,
;    3.43195760762822E+00);
_i_d .int 9695, -9695, 2929, 14057 ;Scaled by 2^-3

;-- state variables
;d_xk : vector (1) of fractional; -- d-current
_d_xk .int 0
;d_xk1 : vector (1) of fractional;
_d_xk1 .int 0
;d_xk1_hp : rawaccumulator;
_d_xk1_hp .long 0

;q_xk : vector (1) of fractional; -- q-current
_q_xk .int 0
;q_xk1 : vector (1) of fractional;
_q_xk1 .int 0
;q_xk1_hp : rawaccumulator;
_q_xk1_hp .long 0

; /* From ACTTRANS.H */
;-- matrix to transform phase currents to current vector in stator frame
;phase_to_stator1 : scalable constant vector (2) of fractional
; := (1.0, 0.0);
; This is not used
;_phase_to_stator1 .int 32767, 0 ;not scaled

;phase_to_stator2 : scalable constant vector (2) of fractional
; := ( 0.577350269, 1.154700538);
_phase_to_stator2 .int 9459, 18919 ;scaled by 2^-1

;-- matrix to transform from stator frame to rotor flux frame
;-- the coefficients are runtime dependent and are
;-- predefined worst case for the scalar product scaling
;stator_rotor1 : scalable constant vector (2) of fractional
; := ( 0.707106781, 0.707106781);
_stator_rotor1 .int 23170, 23170 ;not scaled

```

```

;stator_rotor2 : scalable constant vector (2) of fractional
; := (-0.707106781, 0.707106781);
_stator_rotor2 .int -23170, 23170 ;not scaled

;-- matrix to transform voltage vector in stator frame to phase voltages
;stator_to_phase1 : scalable constant vector (2) of fractional
; := ( 1, 0);
; This is not used
;_stator_to_phase1 .int 32767, 0 ;not scaled

;stator_to_phase2 : scalable constant vector (2) of fractional
; := ( -0.5, 0.866025403);
_stator_to_phase2 .int -16384, 28378 ;not scaled

;stator_to_phase3 : scalable constant vector (2) of fractional
; := ( -0.5, -0.866025403);
_stator_to_phase3 .int -16384, -28378 ;not scaled

;-- intermediate variables
;result : vector (2) of fractional; -- intermediate result vector
_result .int 0, 0
;rotor_voltage : vector (2) of fractional; -- voltage in rotor flux frame
_rotor_voltage .int 0,0

; /*From ACIMOD.H */
;-- system matrices of flux model
;m_a1 : scalable constant vector (2) of fractional
; := ( 9.94247360164699E-01,
; 0.00000000000000E+00);
_m_a1 .int 32579, 0 ;not scaled
;m_a2 : scalable constant vector (2) of fractional
; := ( 0.00000000000000E+00,
; 1.00000000000000E+00);
; This is not used
;_m_a2 .int 0, 32767 ;not scaled
;m_b_1 : scalable constant vector (5) of fractional
; := ( 6.90506233209837E-03,
; 0.00000000000000E+00,
; 0.00000000000000E+00,
; 0.00000000000000E+00,
; 0.00000000000000E+00);
_m_b_1 .int 226, 0, 0, 0, 0 ;not scaled

```

```

;m_b_2 : scalable constant vector (5) of fractional
; := ( 0.000000000000000E+00,
;     4.99999999920422E-02,
;     0.000000000000000E+00,
;     0.000000000000000E+00,
;     0.000000000000000E+00);
_m_b_2 .int 0, 1638, 0, 0, 0 ;not scaled
;m_c_1 : scalable constant vector (2) of fractional
; := ( 9.99999999999999E-01,
;     0.000000000000000E+00);
;_m_c_1 .int 32767, 0 ;not scaled
;MODIFIED FOR NEW TIMING
_m_c_1 .int 32767, 0 ;Scaled by 2^-1
;m_c_2 : scalable constant vector (2) of fractional
; := ( 3.61100000000000E-01,
;     0.000000000000000E+00);
;_m_c_2 .int 11833, 0 ;not scaled
;MODIFIED FOR NEW TIMING
_m_c_2 .int 23665, 0 ;not scaled
;m_c_3 : scalable constant vector (2) of fractional
; := ( 0.000000000000000E+00,
;     9.99999999999999E-01);
;_m_c_3 .int 0, 16384 ;Scaled by 2^-2
;MODIFIED FOR NEW TIMING
_m_c_3 .int 0, 32767 ;Scaled by 2^-2
;m_d_3 : scalable constant vector (5) of fractional
; := ( 0.000000000000000E+00,
;     0.000000000000000E+00,
;     0.000000000000000E+00,
;     2.00000000000000E+00,
;     0.000000000000000E+00);
; This is not used
;_m_d_3 .int 0, 0, 0, 32767, 0 ;scaled by 2^-1
;m_d_4 : scalable constant vector (5) of fractional
; := ( 0.000000000000000E+00,
;     1.00000000000000E+00,
;     1.00000000015916E+00,
;     0.000000000000000E+00,
;     0.000000000000000E+00);
_m_d_4 .int 0, 16384, 16384, 0, 0 ;scaled by 2^-1
;m_d_5 : scalable constant vector (5) of fractional
; := ( 0.000000000000000E+00,
;     0.000000000000000E+00,

```

```

; 1.00000000015916E+00,
; 0.000000000000000E+00,
; 0.000000000000000E+00);
; This is not used
;_m_d_5 .int 0, 0, 32767, 0, 0 ;not scaled
;m_d_6 : scalable constant vector (5) of fractional
; := ( 0.000000000000000E+00,
; 0.000000000000000E+00,
; 0.000000000000000E+00,
; 0.000000000000000E+00,
; 1.59154943096444E-02);
_m_d_6 .int 0, 0, 0, 0, 522 ;not scaled

;-- state variables
;m_xk : vector (2) of fractional; -- flux model
_m_xk .int 0,0
;m_xk1 : vector (2) of fractional;
_m_xk1 .int 0,0

; /* From VEL_CTRL.DSP */
;-- external inputs
;phase_current : vector (2) of fractional;
;input is phase_current;
; i_phase_a renames phase_current (1);
; i_phase_b renames phase_current (2);
_phase_current
_i_phase_a .int 0
_i_phase_b .int 0

;-- current controller inputs
;d_controller_input : vector (4) of fractional;
; i_sd_ref renames d_controller_input (1);
; i_sd renames d_controller_input (2);
; d_decouple renames d_controller_input (3);
_d_controller_input
_i_sd_ref .int 0
_i_sd .int 0
_d_decouple .int 0
.int 0

;q_controller_input : vector (4) of fractional;

```

```

; i_sq_ref    renames q_controller_input (1);
; i_sq       renames q_controller_input (2);
; q_decouple  renames q_controller_input (3);
; psi_decouple renames q_controller_input (4);
_q_controller_input
_i_sq_ref .int 0
_i_sq .int 0
_q_decouple .int 0
_psi_decouple .int 0

;-- controller outputs
;u_sd : fractional;    -- output from d current controller
_u_sd .int 0
;u_sq : fractional;    -- output from q current controller
_u_sq .int 0

;-- phase voltages
;u_a : fractional;
_u_a .int 0
;u_b : fractional;
_u_b .int 0
;u_c : fractional;
_u_c .int 0

;-- phase voltages to compute duty cycles
;u_a_mod : fractional;
_u_a_mod .int 0
;u_b_mod : fractional;
_u_b_mod .int 0
;u_c_mod : fractional;
_u_c_mod .int 0

;-----Vel. Control-----
    .align
; /*From ACCTRL.H */
vel_control:  ; /*here are the variables for the velocity controller*/
;-- system matrices of velocity controller
;-- v_a not necessary --> high precision mode
;v_b : scalable constant vector (2) of fractional
; := ( 1.05998807393070E+00,
;    -1.05998807393070E+00);
;_v_b .int 17367, -17367 ;Scaled by 2^-1
;MODIFIED FOR NEW TIMING

```

_v_b .int 17367*8/25, -17367*8/25 ;Scaled by 2^-1

;v_c : scalable constant vector (1) of fractional

; := (1.000000000000000E+00);

_v_c .int 1024 ; Scaled by 2^-5

;v_d : scalable constant vector (2) of fractional

; := (1.88495559240000E+01,

; -1.88495559240000E+01);

_v_d .int 19302*2/5, -19302*2/5 ;Scaled by 2^-5

-- system matrices of first order lag for velocity reference

;a_v_fol : scalable constant vector (1) of fractional

; := (-4.5412768e-02); -- computed matrix - 1.0 !!!

_a_v_fol .int -1488 ;Not scaled

;b_v_fol : scalable constant vector (1) of fractional

; := (4.49627708289495E-02);

_b_v_fol .int 1473 ;Not scaled

;c_v_fol : scalable constant vector (1) of fractional

; := (9.86896949527394E-01);

_c_v_fol .int 32339 ;Not scaled

;MODIFIED FOR NEW TIMING

_c_v_fol .int 32339 ;Not scaled

;d_v_fol : scalable constant vector (1) of fractional

; := (2.28822623921473E-02);

_d_v_fol .int 750 ;Not scaled

; Filter for velocity value

;fir_coeff : scalable constant vector (5) of fractional

; := (0.2, 0.2, 0.2, 0.2, 0.2);

_fir_coeff .int 6553, 6553, 6553, 6553, 6553

;encoder_counter : vector (2) of fractional;

_encoder_counter .int 0,0

;fir_omega_m : vector (5) of fractional;

_fir_omega_m .int 0, 0, 0, 0, 0

```

;v_xk    : vector (1) of fractional; -- velocity
_v_xk   .int 0
;v_xk1   : vector (1) of fractional;
_v_xk1  .int 0
;v_xk1_hp : rawaccumulator;
_v_xk1_hp .long 0
;qirfs   : fractional;
_qirfs  .int 0

;v_fol_xk : vector (1) of fractional; -- velocity reference first order lag
_v_fol_xk .int 0
;v_fol_xk1 : vector (1) of fractional;
_v_fol_xk1 .int 0
;v_fol_xk1_hp : rawaccumulator;
_v_fol_xk1_hp .long 0

;-- input vectors
;v_fol_u   : vector (1) of fractional; -- for velocity first order lag
_v_fol_u  .int 0

; /* From VEL_CTRL.DSP */
;omega_m_ref   : fractional;      -- reference of rotor velocity
;input is omega_m_ref;
_omega_m_ref  .int 0

;-- velocity controller inputs
;v_controller_input : vector (2) of fractional;
; omega_m_ref_delayed renames v_controller_input (1);
; omega_m         renames v_controller_input (2);
_v_controller_input
_omega_m_ref_delayed .int 0
    .if cls_lp=1
_omega_m_est .int 0
    .else
_omega_m .int 0
    .endif

    .if cls_lp=0 ;defining the other variable outside
_omega_m_est .int 0
    .else

```

```

_omega_m .int 0
    .endif

;-- miscellaneous
;i_sq_max :fractional;
_i_sq_max .int 0

    .globl _u_al, _u_be, _i_al, _i_be
    .globl diff_FI, h, _x, _x_1, diff_h,P, P_1, _K, RSLT, Q, R
    .align

;-----Kalman Filter-----
; New data page for Kalman filter variables
kal_fil

eps_int .long 0
;input vector
U
_u_al .word 0
_u_be .word 0
;output vector
Y
_i_al .word 0
_i_be .word 0

diff_FI .word 25680, 0, 498, 0, 0
        .word 0, 25680, 0, 498, 0
        .word 3675, 0, 32358, 0, 0
        .word 0, 3675, 0, 32358, 0
        .word 0, 0, 0, 0, 32767

_x .word 0, 0, 0, 0, 0

h ;h=[x(1),x(2)]
_x_1 .word 0, 0, 0, 0, 0

diff_h .word 32767, 0, 0, 0, 0
        .word 0, 32767, 0, 0, 0

P .word 0, 0, 0, 0, 0
  .word 0, 0, 0, 0, 0
  .word 0, 0, 0, 0, 0

```

```

        .word 0, 0, 0, 0, 0
        .word 0, 0, 0, 0, 0

P_1    .word 0, 0, 0, 0, 0
        .word 0, 0, 0, 0, 0
        .word 0, 0, 0, 0, 0
        .word 0, 0, 0, 0, 0
        .word 0, 0, 0, 0, 0

Q      .word 0, 0, 0, 0, 80h

R      .word 7000h, 7000h

RSLT   .space 25*16

_K     .word 0, 0
        .word 0, 0
        .word 0, 0
        .word 0, 0
        .word 0, 0

        .text

;-----Macros-----
        .copy "fdiv.inc"      ;fractional division macro

shconst1 .set 4000h
shconst2 .set 6000h
shconst3 .set 7000h
shconst4 .set 7800h
shconst5 .set 7C00h
shconst6 .set 7E00h
shconst7 .set 7F00h

;SATurate Accumulator macro
;performs saturation (1<=Num<=7) before shifting by Num
sata    .macro Num
        setc ovm          ;saturating
        exar
        lacc #shconst:Num:, 15
        sfl
        exar             ; ACCB = constant for saturating

```

```

addb
sbb
sbb
addb
clrc ovm
.endm

```

```

;Round And Saturate Accumulator macro.
;performs rounding and saturation (1<=Num<=7) before shifting by Num

```

```

rasa .macro Num
    add #1, 15-Num ;rounding
    setc ovm ;saturating
    exar
    lacc #shconst:Num:, 15
    sfl
    exar ; ACCB = constant for saturating
    addb
    sbb
    sbb
    addb
    clrc ovm
    .endm

```

```

.copy "matG.inc" ;macros for matrix manipulation

```

```

;-----Routines for the Kalman filter -----

```

```

;*****
;Inputs: i_al, i_be, u_al, u_be
;Outputs: omega_m_est, sin(eps_fs), cos(eps_fs)
.globl _kalman_filter
_kalman_filter:
    ldp #kal_fil
    sar AR0,*+
    sar AR2,*+
    sar AR3,*+
    sar AR4,*+
; % calc. inp and out vec of kalman filter
; U = [u(1); u(2)];
; Y = [u(3); u(4)];

```

```

;   %at this point we have x=x[k-1], U=u[k-1], Y=y[k]????????
;
;   %prediction
;   diff_FI=[1-Kr_K/Kl_K*T, 0, Lh_K*Rr_K/Lr_K/Lr_K/Kl_K*T,
Lh_K/Lr_K*omega_m_scl*x(5)/Kl_K*T, Lh_K/Lr_K*psi_scl*x(4)/Kl_K*T;
;       0, 1-Kr_K/Kl_K*T, -Lh_K/Lr_K*omega_m_scl*x(5)/Kl_K*T,
Lh_K*Rr_K/Lr_K/Lr_K/Kl_K*T,-Lh_K/Lr_K*psi_scl*x(3)/Kl_K*T;
;       Lh_K/Tr_K*T, 0, 1-T/Tr_K, -omega_m_scl*x(5)*T, -psi_scl*x(4)*T;
;       0, Lh_K/Tr_K*T, omega_m_scl*x(5)*T, 1-T/Tr_K, psi_scl*x(3)*T;
;       0, 0, 0, 0, 1]/Q_scl;

```

```

lar  AR2,#_x+4
lar  AR3,#diff_FI+3
mar  *,AR2
lt   *-,AR3      ;Treg=x(5)
mpy  #6256
pac
sach *,1
neg
adrk 4
sach *,1
mpy  #-5147
pac
adrk 6
sach *,1
neg
adrk 4
sach *,1,AR2
lt   *-,AR3      ;Treg=x(4)
mpy  #-5147
pac
sbrk 3
sach *,1
mpy  #6256
pac
sbrk 10
sach *,1,AR2
lt   *,AR3       ;Treg=x(3)
mpy  #-6256
pac
adrk 5
sach *,1
mpy  #5147

```

```

pac
adrk 10
sach *,1
;
;
; x_1=[diff_FI(1,1)*x(1)+diff_FI(1,3)*x(3)+diff_FI(1,4)*x(4);
;   diff_FI(2,2)*x(2)+diff_FI(2,3)*x(3)+diff_FI(2,4)*x(4);
;   diff_FI(3,1)*x(1)+diff_FI(3,3)*x(3)+diff_FI(3,4)*x(4);
;   diff_FI(4,2)*x(2)+diff_FI(4,3)*x(3)+diff_FI(4,4)*x(4);
;   diff_FI(5,5)*x(5)]...
;   +T*[u_s_scl*u(1)/Kl_K; u_s_scl*u(2)/Kl_K; 0; 0; 0]./x_scl;

```

```

spm 1
setc ovm
lar AR4,#_x_1
lar AR2,#_x
lar AR3,#diff_FI
mar *,AR2
lt *+
mar *+,AR3
mpy *+
mar *+,AR2
ltp *+,AR3
mpy *+,AR2
lta *+,AR3
mpy *+,AR2
lar AR2,#U
lta *,AR4
mpy #10749
apac
sach *+,AR2 ;storing in x_1

```

```

lar AR2,#_x+1
lar AR3,#diff_FI+6
lt *+,AR3
mpy *+,AR2
ltp *+,AR3
mpy *+,AR2
lta *+,AR3
mpy *+,AR2
lar AR2,#U+1
lta *,AR4
mpy #10749
apac

```

```

sach  *+,AR2      ;storing in x_1

lar   AR2,#_x
lar   AR3,#diff_FI+10
mar   *,AR2
lt    *+
mar   *+,AR3
mpy   *+
mar   *+,AR2
ltp   *+,AR3
mpy   *+,AR2
lta   *+,AR3
mpy   *+,AR4
apac
sach  *+,AR2      ;storing in x_1

lar   AR2,#_x+1
lar   AR3,#diff_FI+16
lt    *+,AR3
mpy   *+,AR2
ltp   *+,AR3
mpy   *+,AR2
lta   *+,AR3
mpy   *+,AR4
apac
sach  *+,AR2      ;storing in x_1

lar   AR2,#_x+4
lar   AR3,#diff_FI+24
lt    *,AR3
mpy   *,AR4
pac
sach  *,AR2
spm   0
clrc  ovm

;
; P_1=diff_FI*P*diff_FI' + GAM*Q*GAM'; %P[k|k-1] is ready
mmtfraG P, diff_FI, RSLT, 5,5,5
mmfraG diff_FI, RSLT, P_1, 5,5,5
madiG P_1,Q,5

;

```

```

; % calculation of h, diff_h
; h=[x(1); x(2)];
; diff_h=[1 0 0 0 0
;         0 1 0 0 0];
;Nothing to do

; % system of Kalman filter
; K=P_1*diff_h* inv(diff_h*P_1*diff_h'+R); %K[k]
mmfraG P_1, diff_h, RSLT, 5,5,2
mmfraG diff_h, RSLT, _K, 2,5,2 ;_K is yet unused, use as temp
madiG _K, R, 2
madjG _K, P ;P is now unused, use it as temp.
mmfraG RSLT, P, _K, 5, 2, 2
detG P, RSLT ; supposing, that det(RSLT)<1
mdsc1G _K, RSLT, _K, 5, 2, RSLT+1

; sys = x_1+K*(Y-h); %x[k] is ready
msubG Y, h, P, 2,1 ;use P as temp
mmfraG _K, P, RSLT, 5,2,1
maddG _x_1, RSLT, _x, 5,1
; P=P_1-K*diff_h*P_1; %P[k] is ready
mmfraG _K, diff_h, RSLT, 5, 2, 5
mmfraG RSLT, P_1, P, 5, 5, 5
msubG P_1,P,P,5,5

;We need an additional integrator to calculate eps_RS_est
ldp #kal_fil
lacc _x+4
ldp #vel_control
sac1 _omega_m_est

;Calculation of sin(eps_fs) and cos(eps_fs) from psi_r_al, und psi_r_be
vnormG _x+2,_stator_rotor1, RSLT
ldp #cur_control
lacc _stator_rotor1
or _stator_rotor1+1
bcnd ok_k, NEQ
lacc #32767
sac1 _stator_rotor1
ok_k
lacc _stator_rotor1
sac1 _stator_rotor2+1
lacc _stator_rotor1+1

```

```

neg
sac1  _stator_rotor2

k_epi
mar  *,AR1
mar  *-
lar  AR4,*-
lar  AR3,*-
lar  AR2,*-
lar  AR0,*
ret

```

```

;-----Routines for the velocity control-----

```

```

;*****
;Inputs: v_controller_input
; i_sq_max
;Output: i_sq_ref
    .globl _v_control
_v_control:
    ldp  #vel_control
; update (v_xk1, v_xk);
    lacc  _v_xk1
    sac1  _v_xk

; accumulate scalpro (controller_out_scp)
; qirfs := v_c * v_xk1 + v_d * _v_controller_input;
; end accumulate;
    lt  _v_c
    mpy  _v_xk1
    ltp  _v_d
    mpy  _v_controller_input
    lta  _v_d+1
    mpy  _v_controller_input+1
    apac
    rasa  6
    sach  _qirfs, 6

; if ABS (qirfs) <= i_sq_max then
; accumulate prescalpro (controller_state_scp)
; v_xk1_hp := v_xk1_hp + v_b * v_controller_input;
; end accumulate;

```

```

; end if;
  lacc  _qirfs
  sub   _i_sq_max
  bcnd  overrun, GT
  lacc  _qirfs
  add   _i_sq_max
  bcnd  underrun, LT

  lacc  _v_xk1_hp, 16
  clrc  sxm
  add   _v_xk1_hp+1
  setc  sxm
  lt    _v_b
  mpy   _v_controller_input
  lta   _v_b+1
  mpy   _v_controller_input+1
  apac
  sata  2
  sach  _v_xk1_hp ;not correcting after Q15 multipl.
  sacl  _v_xk1_hp+1 ; here.
; accumulate prescalpro (controller_state_scp)
; v_xk1 (1) := v_xk1_hp;
; end accumulate ;
  sach  _v_xk1, 2

  b    ok_v

```

```

overrun
  lacc  _i_sq_max
  sacl  _qirfs
  b    comp

```

```

underrun
  lacc  _i_sq_max
  neg
  sacl  _qirfs

```

```

comp
  lacc  _qirfs, 10
  lt    _v_d
  mpy   _v_controller_input
  lts   _v_d+1

```

```

    mpy  _v_controller_input+1
    spac
    sach _v_xk1, 6
    sach _v_xk1_hp,4
    sacl _v_xk1_hp+1,4

ok_v
    ldp  #_pwmon
    lacc _pwmon
    ldp  #vel_control
    bcnd on0,GT
    lacc #0
    sacl _v_xk1_hp
    sacl _v_xk1_hp+1
    sach _v_xk1
    sacl _qirfs

on0

    lacc _qirfs
    ldp  #cur_control
    sacl _i_sq_ref

    ret

;*****
;Input:  _omega_m_ref
;Output: _omega_ref_delayed
    .globl _v_first_order_lag
_v_first_order_lag:
    ldp  #vel_control
; v_fol_u (1) := v_ref_in;
    lacc _omega_m_ref
    sacl _v_fol_u

; update (v_fol_xk1, v_fol_xk);
    lacc _v_fol_xk1
    sacl _v_fol_xk

; accumulate scalpro (v_fol_out_scp)
; omega_m_ref_delayed := c_v_fol * v_fol_xk1 + d_v_fol * v_fol_u;
; end accumulate;

```

```

lt _c_v_fol
mpy _v_fol_xk1
ltp _d_v_fol
mpy _v_fol_u
apac
rasa 1
sach _omega_m_ref_delayed,1

```

```
; -- delay replacement to avoid quantization effects
```

```
; accumulate prescalpro (v_fol_state_scp)
; v_fol_xk1_hp := v_fol_xk1_hp + a_v_fol * v_fol_xk + b_v_fol * v_fol_u;
; end accumulate;
    lacc _v_fol_xk1_hp, 16
    clrc sxm
    add _v_fol_xk1_hp+1
    setc sxm
    lt _a_v_fol
    mpy _v_fol_xk
    lta _b_v_fol
    mpy _v_fol_u
    apac
    sata 1
    sach _v_fol_xk1_hp ;not correcting after Q15 multipl.
    sacl _v_fol_xk1_hp+1 ;here.

```

```
; accumulate prescalpro (v_fol_state_scp)
; v_fol_xk1 (1) := v_fol_xk1_hp;
; end accumulate
    sach _v_fol_xk1, 1
    ldp #_pwmon
    lacc _pwmon
    ldp #vel_control
    bcnd on1,GT
    lacl #0
    sacl _v_fol_xk1_hp
    sacl _v_fol_xk1_hp+1
    sacl _v_fol_xk1
    sacl _omega_m_ref_delayed

```

```
on1
```

ret

;-----Routines for the current control-----

.globl _q_control

_q_control:

ldp #cur_control

; update (q_xk1, q_xk);

lacc _q_xk1

sac1 _q_xk

; accumulate scalpro (controller_out_scp)

; u_sq := i_c * q_xk1 + i_d * q_controller_input;

; end accumulate;

lt _i_c

mpy _q_xk1

ltp _i_d

mpy _q_controller_input

lta _i_d+1

mpy _q_controller_input+1

lta _i_d+2

mpy _q_controller_input+2

lta _i_d+3

mpy _q_controller_input+3

apac

rasa 4 ;Saturating before shifting

sach _u_sq, 4

; accumulate prescalpro (controller_state_scp)

; q_xk1_hp := q_xk1_hp + i_b * q_controller_input;

; end accumulate;

lacc _q_xk1_hp, 16

clrc sxm

add _q_xk1_hp+1

setc sxm

lt _i_b

mpy _q_controller_input

lta _i_b+1

mpy _q_controller_input+1

; i_b[2] and i_b[3] == 0, so we do not multiply them here.

apac

sata 1

```
sach  _q_xk1_hp  ; not correcting after Q15 multipl.
sac1  _q_xk1_hp+1 ; here.
```

```
; accumulate prescalpro (controller_state_scp)
```

```
; q_xk1 (1) := q_xk1_hp;
```

```
; end accumulate
```

```
    sach  _q_xk1,1
    ldp   #_pwmon
    lacc  _pwmon
    ldp   #cur_control
    bcnd  on2,GT
    lacl  #0
    sac1  _q_xk1_hp
    sac1  _q_xk1_hp+1
    sac1  _q_xk1
    sac1  _u_sq
```

```
on2
```

```
    ret
```

```
.;*****
```

```
;Input: _d_controller_input
```

```
;Output: _u_sd
```

```
    .globl _d_control
```

```
_d_control:
```

```
    ldp   #cur_control
```

```
; update (d_xk1, d_xk);
```

```
    lacc  _d_xk1
```

```
    sac1  _d_xk
```

```
; accumulate scalpro (controller_out_scp)
```

```
; u_sd := i_c * d_xk1 + i_d * d_controller_input1;
```

```
; end accumulate;
```

```
    lt  _i_c
```

```
    mpy  _d_xk1
```

```
    ltp  _i_d
```

```
    mpy  _d_controller_input
```

```
    lta  _i_d+1
```

```
    mpy  _d_controller_input+1
```

```
    lta  _i_d+2
```

```
    mpy  _d_controller_input+2
```

```

lta _i_d+3
mpy _d_controller_input+3
apac
rasa 4
sach _u_sd,4

; accumulate prescalpro (controller_state_scp)
; d_xk1_hp := d_xk1_hp + i_b * d_controller_input;
; end accumulate;
lacc _d_xk1_hp, 16
clrc sxm
add _d_xk1_hp+1
setc sxm
lt _i_b
mpy _d_controller_input
lta _i_b+1
mpy _d_controller_input+1
; i_b[2] and i_b[3] == 0, so we do not multiply them here.
apac
sata 1
sach _d_xk1_hp ;not correcting after Q15 multipl.
sac1 _d_xk1_hp+1 ;here.

; accumulate prescalpro (controller_state_scp)
; d_xk1 (1) := d_xk1_hp;
; end accumulate
sach _d_xk1, 1
ldp #_pwmon
lacc _pwmon
ldp #cur_control
bcnd on3,GT
lac1 #0
sac1 _d_xk1_hp
sac1 _d_xk1_hp+1
sac1 _d_xk1
sac1 _u_sd

on3

ret

```

```

;*****
;Inputs: _eps_fs
;  _phase_current
;Outputs:_i_sd
;  _i_sq
      .globl _phase_to_rotor
_phase_to_rotor:
      ldp    #cur_control

; -- set input vector
; -- transform phase to stator frame
; accumulate scalpro (transformation_scp)
; result (1) := phase_to_stator1 * phase_current;
; end accumulate;
      lacc _phase_current
      ; we do not multiply by phase_to_stator[0], because it is 1
      ; we do not use phase_to_stator[1], because it is 0
      sacl _result
      ldp    #kal_fil
      sacl  _i_al
      ldp    #cur_control

; accumulate scalpro (transformation_scp)
; result (2) := phase_to_stator2 * phase_current;
; end accumulate;
      lt    _phase_to_stator2
      mpy  _phase_current
      ltp  _phase_to_stator2+1
      mpy  _phase_current+1
      apac
      rasa 2
      sach _result+1, 2
      ldp  #kal_fil
      sach _i_be,2
      ldp  #cur_control

; -- transform stator frame to rotor flux frame
; accumulate scalpro (transformation_scp)
; i_sd := stator_rotor1 * result;

```

```

; end accumulate;
    lt  _stator_rotor1
    mpy _result
    ltp _stator_rotor1+1
    mpy _result+1
    apac
    rasa 1
    sach  _i_sd, 1

; accumulate scalpro (transformation_scp)
;  i_sq := stator_rotor2 * result;
; end accumulate
    lt  _stator_rotor2
    mpy _result
    ltp _stator_rotor2+1
    mpy _result+1
    apac
    rasa 1
    sach  _i_sq, 1

ret

;*****
;Inputs:  u_sd
;   u_sq
;Outputs: u_a
;   u_b
;   u_c
    .globl _rotor_to_phase
_rotor_to_phase:
    ldp  #cur_control
; -- set input vector
; rotor_voltage (1) := u_sd;
; rotor_voltage (2) := u_sq;
    lacc  _u_sd
    sacl  _rotor_voltage
    lacc  _u_sq
    sacl  _rotor_voltage+1

; -- get inverse of matrix stator_rotor
; -- by transposition (swapping elements (2,1) and (1,2))

```

```

; dummy := stator_rotor2 (1);
; stator_rotor2 (1) := stator_rotor1 (2);
; stator_rotor1 (2) := dummy;
  lacc  _stator_rotor2
  sacb
  lacc  _stator_rotor1+1
  sacl  _stator_rotor2
  lacb
  sacl  _stator_rotor1+1

; -- transform rotor flux frame to stator frame
; accumulate scalpro (transformation_scp)
; result (1) := stator_rotor1 * rotor_voltage;
; end accumulate;
  lt  _stator_rotor1
  mpy _rotor_voltage
  ltp _stator_rotor1+1
  mpy _rotor_voltage+1
  apac
  rasa  1
  sach  _result, 1
  ldp  #kal_fil
  sach  _u_al, 1
  ldp  #cur_control

; accumulate scalpro (transformation_scp)
; result (2) := stator_rotor2 * rotor_voltage;
; end accumulate;
  lt  _stator_rotor2
  mpy _rotor_voltage
  ltp _stator_rotor2+1
  mpy _rotor_voltage+1
  apac
  rasa  1
  sach  _result+1, 1
  ldp  #kal_fil
  sach  _u_be, 1
  ldp  #cur_control

; -- transform stator frame to phase
; accumulate scalpro (transformation_scp)
; u_a := stator_to_phase1 * result;
; end accumulate;

```

```

    lacc _result
    ; _stator_to_phase1 = { 1, 0 } !!
    sacl  _u_a

; accumulate scalpro (transformation_scp)
;  u_b := stator_to_phase2 * result;
; end accumulate;
    lt  _stator_to_phase2
    mpy _result
    ltp _stator_to_phase2+1
    mpy _result+1
    apac
    rasa  1
    sach  _u_b, 1

; accumulate scalpro (transformation_scp)
;  u_c := stator_to_phase3 * result;
; end accumulate
    lt  _stator_to_phase3
    mpy _result
    ltp _stator_to_phase3+1
    mpy _result+1
    apac
    rasa  1
    sach  _u_c, 1

    ret

;-----Peripheral routines-----
    .globl _to_pwm
_to_pwm:
    ldp  #cur_control
    lt   _pwm_period_reg

;we have to push parameters in REVERSE order!!

    lacc #0          ; dummy parameter (bvec)
    sacl *+

    mpy  _u_c_mod
    pac

```

```
add  _pwm_period_reg, 15 ; += period/2
sach *+          ;stack = (period * (1 + u_a_mod)) /2
```

```
mpy  _u_b_mod
pac
add  _pwm_period_reg, 15 ; += period/2
sach *+          ;stack = (period * (1 + u_a_mod)) /2
```

```
mpy  _u_a_mod
pac
add  _pwm_period_reg, 15 ; += period/2
sach *+          ;stack = (period * (1 + u_a_mod)) /2
```

```
call _send_to_pwm ;library function for pwm handling
sbrk #4          ;restoring stack
RET
```

```
.globl _gpio_incr
_gpio_incr
in    *,GPIOINC
lacc  *
ret
```

```
.globl _input_omega_m
_input_omega_m:
; -- read encoder counter
; input (encoder_counter (1));
call  _gpio_incr

ldp  #vel_control
sac1 _encoder_counter
```

```
; -- compute current velocity
; accumulate scalpro (counter_scp) and update encoder_counter
; fir_omega_m (1) := encoder_to_velocity * encoder_counter;
; end accumulate;
lacc  _encoder_counter
sub   _encoder_counter+1
dmov  _encoder_counter
sac1  _encoder_counter
; the velocity is multiplied by 32
```

```

;   sac1  _fir_omega_m, 5
;MODIFIED FOR NEW TIMING
; the velocity is multiplied by 32*1.25
    lt   _encoder_counter
    mpy  #20480 ;1.25/2
    pac
    sach  _fir_omega_m, 7

; -- filter current velocity
; accumulate scalpro (fir_scp) and update fir_omega_m
; velocity := fir_coeff * fir_omega_m;
; end accumulate
    zap
    lt   _fir_omega_m+4
    mpy  _fir_coeff+4
    ltd  _fir_omega_m+3
    mpy  _fir_coeff+3
    ltd  _fir_omega_m+2
    mpy  _fir_coeff+2
    ltd  _fir_omega_m+1
    mpy  _fir_coeff+1
    ltd  _fir_omega_m
    mpy  _fir_coeff
    apac
    rasa 1
    sach  _omega_m, 1
    ret

```

```

;-----Setup routines-----

```

```

;!!! THIS MIGHT BE NEEDED LATER
;   LACC  #0101H
;   SACL  temp
;   OUT   temp, GPIOCRIO1  ; Sending a 1 to the DIG0 of the GPIO
                        ; This pin is connected to the PROT of the motor
                        ; driver card, and it enables all PWM channels
                        ; in the motor

```

```

_timer_init:

```

```
.globl _timer_init
lacc #10000 ;timer interrupt in every 500 us
samm PRD
lacc #100000b ;divide down = 1, load tim from prd
samm TCR
ret
```

```
_intr_init:
```

```
.globl _intr_init
ldp #cur_control
clrc cnf
lacc #830h
samm PMST
lacc #5
sac1 counter
call _timer_init
```

```
lacc #8 ; enable only timer interrupt
samm IMR
eint ; enable interrupts
ret
.end
```

; Kalman Filter for the TMS320C5x

; vel_ctr.c

; Author : Balazs Simor

; Date : June, 1996

#include <stdlib.h>

#include <uart.h>

#include <conio.h>

#include <board.h>

#include <ad.h>

#include <incr.h>

#include <pwm.h>

#include <gpio.h>

int sine(int angle);

#define I_SD_REF_K 6554 /*=frac(0.20) scaled reference for d_current component => 2.0 A*/

#define I_SQ_MAX_K 13107 /*=frac(0.40) scaled maximum for q_current component => 4.0 A*/

#define PWM_PERIOD 600 /* period of PWM generating*/

long int UART_freq=4915200; /* 4.9152 MHz */

char *header="Field oriented velocity control with Kalman filter\r";

int spd=0; /* speed reference */

int pwmon=0; /* turns pwm on and off*/

long pwmsc = 0;

/*-----External variables-----*/

#define extasm(varname) \

extern int varname;\

int *P##varname = &varname;

extasm(omega_m_ref)

extasm(omega_m_ref_delayed)

extasm(i_sq_max)

extasm(i_sq_ref)

extasm(i_sd_ref)

extasm(phase_current)

extasm(i_sd)

extasm(i_sq)

```
extasm(u_sd)
extasm(u_sq)
extasm(omega_m)
extasm(omega_m_est)
extasm(d_decouple)
extasm(q_decouple)
extasm(psi_decouple)
extasm(u_a)
extasm(u_b)
extasm(u_c)
extasm(u_al)
extasm(u_be)
extasm(i_al)
extasm(i_be)
extasm(u_a_mod)
extasm(u_b_mod)
extasm(u_c_mod)
extasm(pwm_period_reg)
extasm(x)
extasm(x_1)
extasm(K)
```

```
/*-----Interrupt handling-----*/
```

```
int xxx = 0;
```

```
void current_control(void)
```

```
{
/*This is the main current control routine. Called from the interrupt rtn.*/
```

```
/*; -- get phase currents*/
```

```
  Pphase_current[0] = (get_ad_val(0)+34-512)<<6;
```

```
  Pphase_current[1] = (get_ad_val(1)+36-512)<<6;
```

```
/* transform phase currents to rotorflux frame*/
```

```
  phase_to_rotor (/*eps_fs, phase_current, i_sd, i_sq*/);
```

```
/* calculate decoupling value d_component*/
```

```
/* *Pd_decouple = (- (long)(*Pi_sq) * (long)(*Pomega_fs))>>15;*/
```

```
/* PI-controller for d-current*/
```

```
  d_control (/*d_controller_input, u_sd*/);
```

```

/* calculate decoupling value q_component*/
/* *Pq_decouple = ((long)(*Pi_sd) * (long)(*Pomega_fs))>>15;
   *Ppsi_decouple = ((long)(*Pomega_rs) * (long)(*Ppsi_rd))>>15;*/

/* PI-controller for q-current*/
q_control (/*q_controller_input, u_sq*/);

/* transform voltage vector from rotorflux frame to phase voltages*/

/* *Pu_sd = 2000;
   *Pu_sq = 0;*/
rotor_to_phase (/*u_sd, u_sq, u_a, u_b, u_c*/);

/* xxx += 10;
   *Pu_a = sine(xxx)/5;
   *Pu_b = sine(xxx-21845)/5;
   *Pu_c = sine(xxx-43691)/5;*/
/* *Pu_a = 30000;
   *Pu_b = -15000;
   *Pu_c = -15000;*/

/* phases a and b are swapped !!! */
*Pu_a_mod = *Pu_b;
*Pu_b_mod = *Pu_a;
*Pu_c_mod = *Pu_c;

to_pwm();
kalman_filter(); /*IN: u_al, u_be, i_al, i_be
                  OUT: omega_m_est*/
}

void speed_control(void)
{
/*This routine does the velocity control. It is called from the interrupt
routine.*/
/*; input (omega_m_ref); -- get velocity reference from communication address
   ; This will be given by the user, and will be in a variable.*/

input_omega_m (/*omega_m*/); /*get position counter and compute rotor velocity*/
/* this will be measured by the incremental encoder interface in the

```

```

    GPIO */

/* first order lag to delay velocity reference*/
v_first_order_lag (/*omega_m_ref, omega_m_ref_delayed*/);

/* PI - controller for rotor velocity*/
v_control (/*i_sq_max, v_controller_input, i_sq_ref*/);
}

void c_int4(void) /*main interrupt handler routine */
{
static int co=0; /* counter for calling speed controller */

    current_control(); /*every 500us*/
    if (0 == (co=(++co)%2))
        speed_control(); /*every 1ms */
}

void init_control(void)
{
    *Pomega_m_ref = 0; /* clear omega_m_ref*/
    *Pi_sq_max = I_SQ_MAX_K; /* q current maximum*/
    *Pi_sd_ref = I_SD_REF_K; /* d current reference is constant*/
}

void init_hardware(void)
{
    ws_init(); /*setting up wait-states for the board */
    *Ppwm_period_reg = PWM_PERIOD;
    pwm_init(M_SYMM, EN_ALL, CHM_SET, CHM_SET, CHM_SET, SW_HARD,
        LOW, LOW, LOW, LOW, 0, PWM_PERIOD, DIR_POS, 0);
/* gpio_init(15L, CLK_DIV1, 0, 0, CLK_DIV1,
CAP_DSBL,CAP_DSBL,CAP_DSBL,CAP_DSBL,
0);*/
    ad_init();
    incr_init();
    uart_init(((UART_freq*10)/16/9600+5)/10);
    intr_init();
}

void setspeed()
{
    clrscr();
}

```

```

    sendstr(header);
    sendstr("\r");
    spd = inputval("Enter speed value", spd, -3000, 3000);
    *Pomega_m_ref = (int)((long)spd*32767/3000);
}

```

```

void speedtest(void)
{
char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rSpeed of the motor: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
            val = (int)((long)(*Pomega_m) * 3000/32767);
            ltoa ((long)val, str);
            sendstr("\b\b\b\b\b\b\b");
            for (i=strlen(str); i<7; i++)
                sendstr(" ");
            sendstr(str);
        } /* for */
}

```

```

void i_sqtest(void)
{
/*char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rValue of variable i_sq: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
            ltoa ((long)(*Pi_sq), str);
            sendstr("\b\b\b\b\b\b\b");

```

```

        for (i=strlen(str); i<7; i++)
            sendstr(" ");
        sendstr(str);
    }*/
}

void i_sdtest(void)
{
/*char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rValue of variable i_sd: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
        ltoa ((long)(*Pi_sd), str);
        sendstr("\b\b\b\b\b\b\b\b");
        for (i=strlen(str); i<7; i++)
            sendstr(" ");
        sendstr(str);
        } */
}

void incrttest(void)
{
/*char str[20];
unsigned val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rInput from the incremental encoder interface: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
        val = get_incr();
        ltoa ((unsigned long)val, str);
        sendstr("\b\b\b\b\b\b\b\b");
        for (i=strlen(str); i<7; i++)
            sendstr(" ");
        }
}

```

```

        sendstr(str);
    } /*
}

void adtest(int ch)
{
char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rInput from the AD converter: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
            val = Pphase_current[ch];
            ltoa ((long)val, str);
            sendstr("\b\b\b\b\b\b\b\b");
            for (i=strlen(str); i<7; i++)
                sendstr(" ");
            sendstr(str);
        } /* for */
}

void varrest(void)
{
/*char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rVariable: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
            val = *Pomega_fr;
            val = Px[0];
            ltoa ((long)val, str);
            sendstr("\b\b\b\b\b\b\b\b");

```

```

{
char str[20];
int val;
int i;
char c;
int co;

    co = 400;
    *Pomega_m_ref=0;
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
        if (--co)
            {
            co=60;
            *Pomega_m_ref=(*Pomega_m_ref==10923 ? -10923 : 10923);
            }
        val = *Pomega_m;
        ltoa ((long)val, str);
        sendstr(str);
        sendstr(",");
        val = *Pomega_m_ref_delayed;
        ltoa ((long)val, str);
        sendstr(str);
        sendstr(",");
        }
}

```

```

void estspdtest(void)
{
char str[20];
int val;
int i;
char c;

    clrscr();
    sendstr(header);
    sendstr("\rEstimated speed of the motor: 0000000");
    for (c=0; c==0; c = (kbhit() ? getch() : 0) )
        {
        val = (int)((long)(*Pomega_m_est) * 3000/32767);
        ltoa ((long)val, str);
        sendstr("\b\b\b\b\b\b\b");
        for (i=strlen(str); i<7; i++)

```

```

        sendstr(" ");
        sendstr(str);
    } /* for */

}

void runmenu(void)
{
char c;
int val, i;
char b[10]="";
    for (;;)
    {
        clrscr();
        sendstr(header);
        sendstr("\rMain Menu\r");
        sendstr("\t1) Set speed reference (currently: ");
        ltoa ((long)spd, b);
        sendstr(b);
        sendstr("\r\t2) See encoder input\r\t3) See current \"a\"\r"
            "\t4) See current \"b\"\r\t5) See measured speed\r"
            "\t6) Turn PWM generating ");
        sendstr(pwmon ? "OFF" : "ON");
        sendstr("\r\t7) See i_sq\r\t8) Measurement Mode"
            "\r\t9) See estimated speed\r\tA) Vartest"
            "\r\tB) See i_sd"
            "\r\tC) See i_al, i_be, u_al, u_be"
            "\rPlease make your choice\r");
        for (c = 0; (c<'1' || c>'9') && (c<'A' || c>'C');c = toupper(uartgetc()));
        switch (c)
        {
            case '1': setspeed(); break;
            case '2': incrtest(); break;
            case '3': adtest(0); break;
            case '4': adtest(1); break;
            case '5': speedtest(); break;
            case '6': pwmon = 1-pwmon; break;
            case '7': i_sqtest(); break;
            case '8': msrmnt(); break;
            case '9': estspdtest(); break;
            case 'A': vartest(); break;
            case 'B': i_sdtest(); break;
            case 'C': al_be_test(); break;
        }
    }
}

```

```
        } /* switch */  
    }  
}
```

```
void main(void)  
{  
    init_control();  
    init_hardware();  
    runmenu();  
}
```

```
; Kalman Filter for the TMS320C5x
; sin.asm
; Author : Balazs Simor
; Date : June, 1996
```

```
.globl _sine
```

```
.data
sintab: .include sine.tab
tabend:
.word 0
```

```
tabsize .set tabend - sintab
```

```
.even
temp .word 0
temp1 .word 0
tempAR3 .word 0
```

```
.text
```

```
*****
```

```
* int sine(int angle);
```

```
*****
```

```
_sine
```

```
ldp #temp
```

```
mar *-
```

```
lacc *+
```

```
sac1 temp
```

```
lt temp
```

```
mpy #tabsize
```

```
pac
```

```
sac1 temp1 ; fractional part of place in table in +Q16 format.
```

```
bsar 16 ; position in table is in ACC
```

```
bcnd poz, GEQ
```

```
add #tabsize
```

```
poz: add #sintab ; address of lower value in ACC
```

```
sac1 temp
```

```
sar AR3, tempAR3
```

```
lar AR3, temp
```

```
mar *, AR3
```

```
mar *+ ; address of higher value in AR3
```

```
lacc temp1, 14 ; converting +Q16 to Q15
```

```
and    #0FFFFh, 14
sach   temp1, 1
lt     *-    ; higher value
mpy    temp1
lacc   #32767
sub    temp1    ; acc = 1-temp1
sac1   temp1
ltp    *, AR1 ;lower value
mpy    temp1
apac
bsar   15    ; The interpolated output is in Acc
lar    AR3, tempAR3 ;restoring AR3
ret
.end
```

